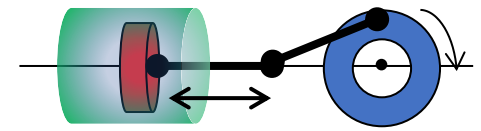
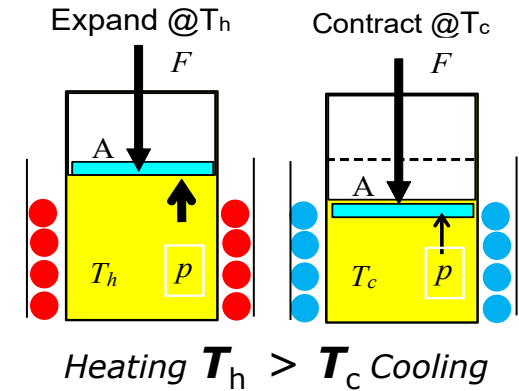
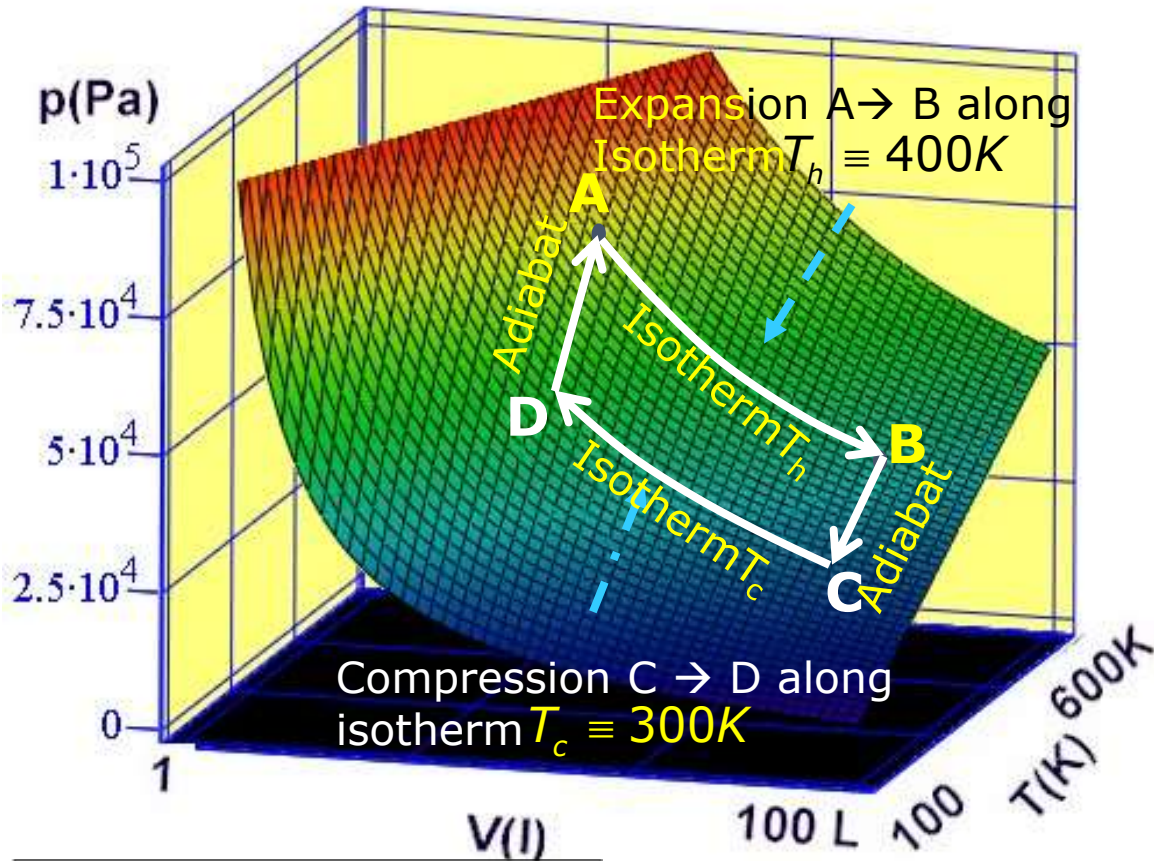


# Reversible Circular Processes on EoS Hyperplane

$$P \cdot V = R \cdot T \quad \text{OR} \quad P \cdot V^\gamma = \text{const}; T \cdot V^{\gamma-1} = \text{const}$$

For  $T = \text{const.}$                       For  $q = 0$

Circular, reversible process  
 $A \rightarrow B \rightarrow C \rightarrow D \rightarrow A$   
 on the EoS hyperplane



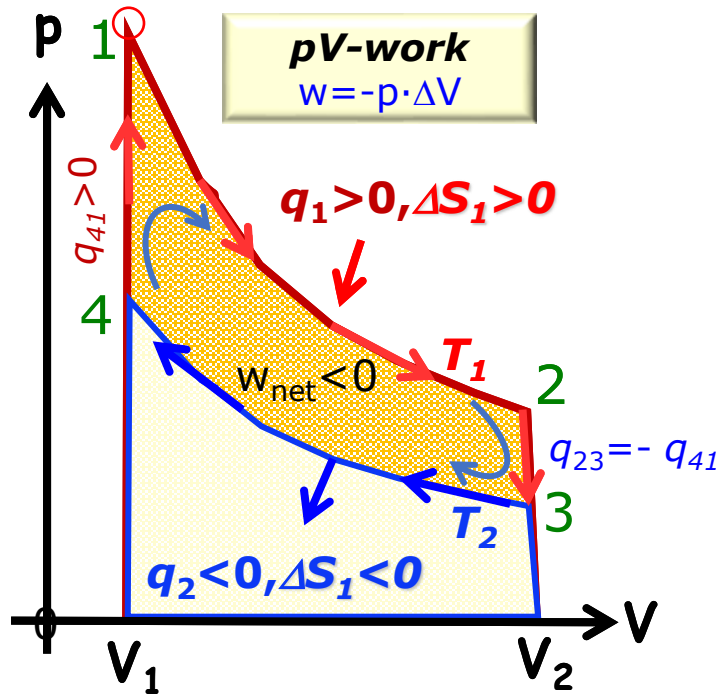
returns the IG system to its initial state A after a combination of slow (=reversible) expansion and compression processes.

Heat and cool the working IG volume @ specific times  $\rightarrow$  Cyclic thermal engine

Ideal Gas Constant  $R$   
 $R = 0.0821 \text{ liter}\cdot\text{atm}/\text{mol}\cdot\text{K}$   
 $R = 8.3145 \text{ J}/\text{mol}\cdot\text{K}$

# Thermal Engine with *Ideal* Working Medium

Ideal-gas system (N particles) in alternating contact with **Heat Bath @  $T_1$**  and **Cold Sink @  $T_2 < T_1$**   $EoS : p \cdot V = N \cdot k_B \cdot T$



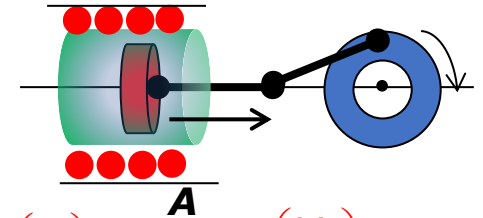
Isochoric legs: No net heat transfer → no change net  $\Delta S$

**Heat energy transfer**

$$q_i = (T \cdot \Delta S)_i; \Delta S = |\Delta S_i|$$

1→2 Isothermal expansion @  $T_1 = \text{const}$

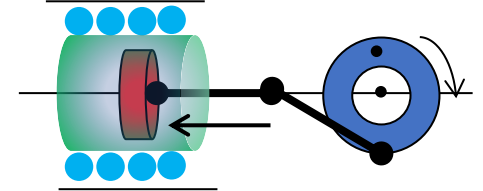
$$w_1 = -\int_{V_1}^{V_2} p(V, T) dV = Nk_B T_1 \cdot \ln(V_1/V_2)$$



$$\frac{w_1}{T_1} = Nk_B \ln\left(\frac{V_1}{V_2}\right) = \frac{-q_1}{T_1} \rightarrow \left(\frac{q}{T}\right)_1 = Nk_B \ln\left(\frac{V_2}{V_1}\right) = \Delta S_1$$

3→4 Isothermal compression @  $T_2 < T_1$

$$w_2 = -\int_{V_2}^{V_1} p(V, T) dV = -Nk_B T_2 \cdot \ln(V_1/V_2)$$

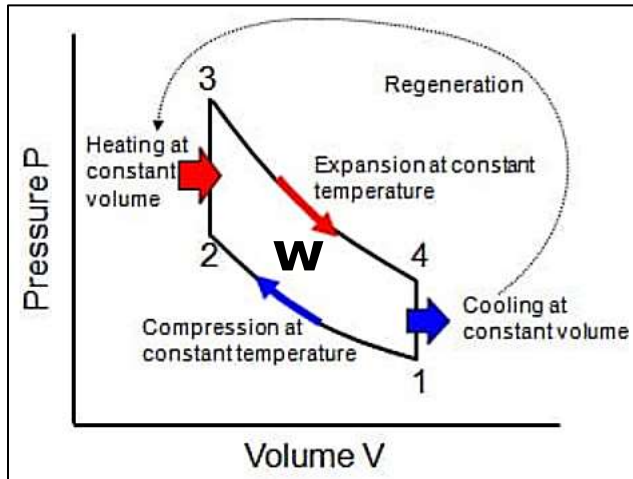


$$\frac{w_2}{T_2} = Nk_B \ln\left(\frac{V_2}{V_1}\right) = \frac{-q_2}{T_2} \rightarrow \left(\frac{q}{T}\right)_2 = Nk_B \ln\left(\frac{V_1}{V_2}\right) = \Delta S_2$$

$$\Delta S_1 = -\Delta S_2 \equiv \Delta S$$

**Cyclic path conserves S(1) Entropy = State<sub>2</sub> Fcn**

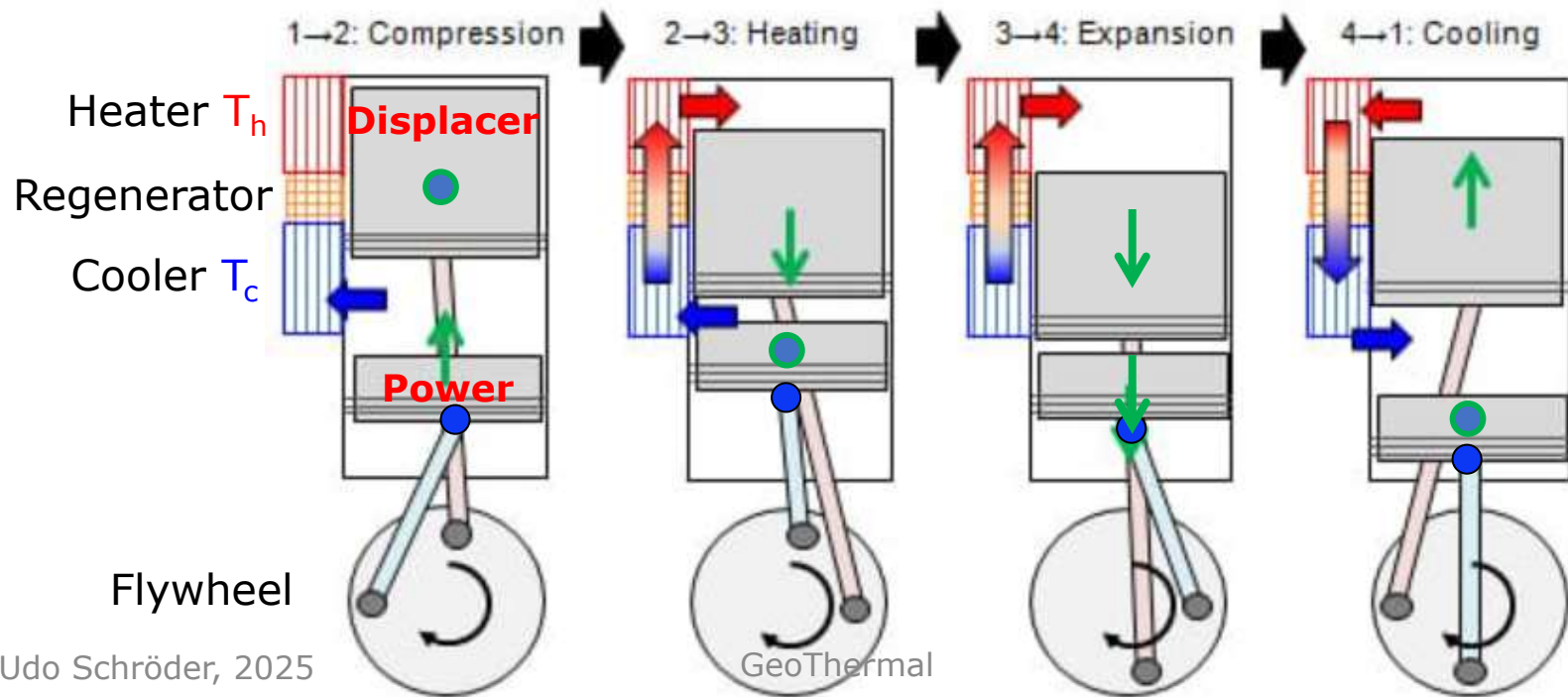
# Stirling Heat Engine ( $\beta$ )



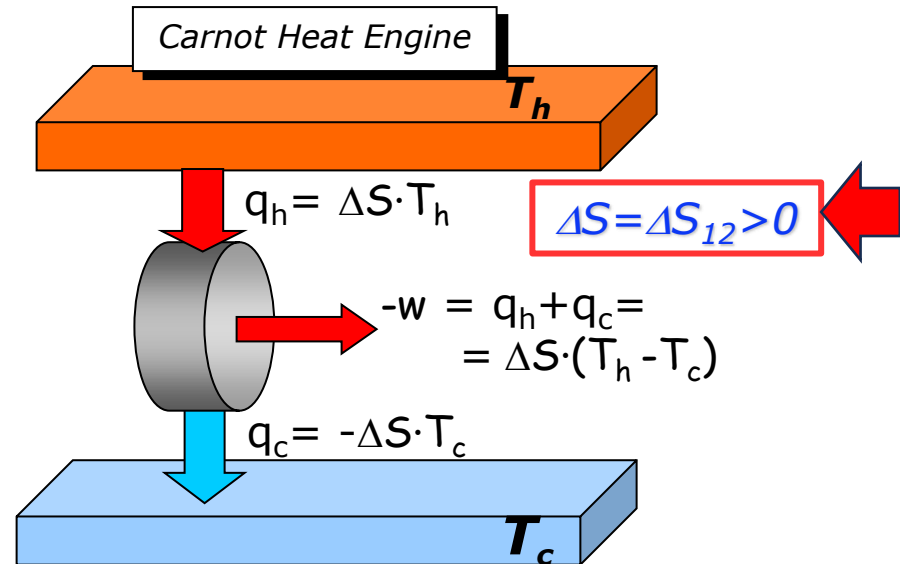
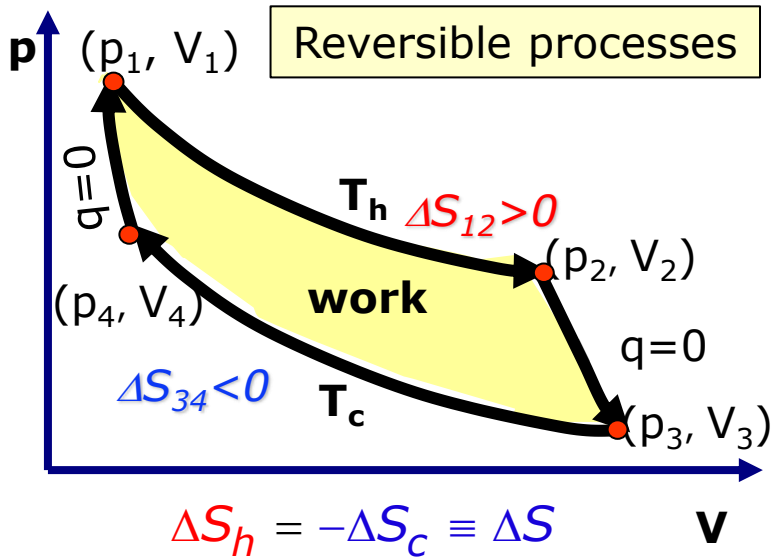
Closed-cycle regenerative heat engine with self-contained, permanent working fluid/gas. Displacer directs flow of working gas between hot and cold spaces.

**Stirling engine** driven by  $T$  gradient, e.g., solar radiation, nuclear decay heat.

**Applications:** concentrated solar insolation, submarines, space craft,..



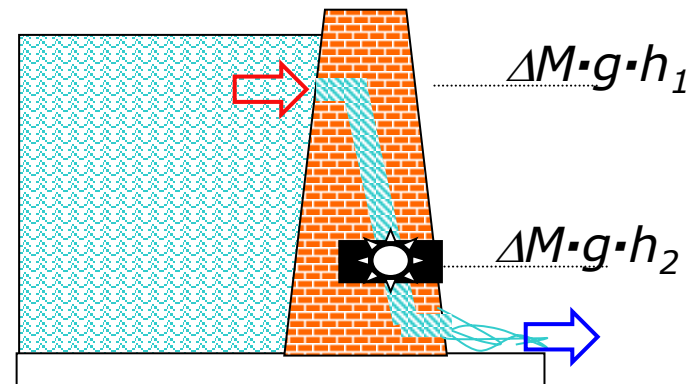
# Entropy Flow in Carnot Engines



$$\varepsilon = \frac{-w}{q_h} = \frac{q_h + q_c}{q_h}$$

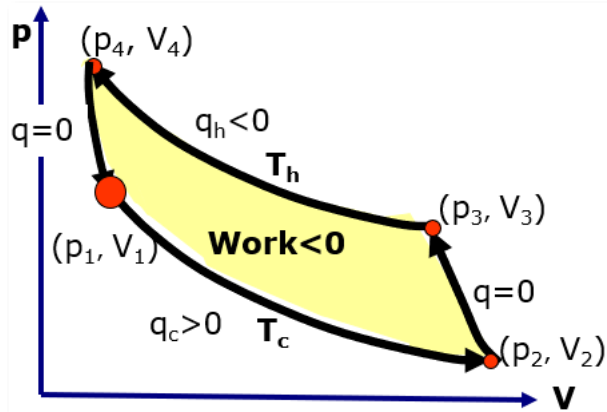
$$\varepsilon = 1 + \frac{q_c}{q_h} = 1 - \frac{T_c}{T_h} \xrightarrow{T_h \rightarrow \infty} 1$$

Hydrodynamic Power Plant



Water stream from reservoir carries energy driving an electric generator.

# Residential Heat Pump

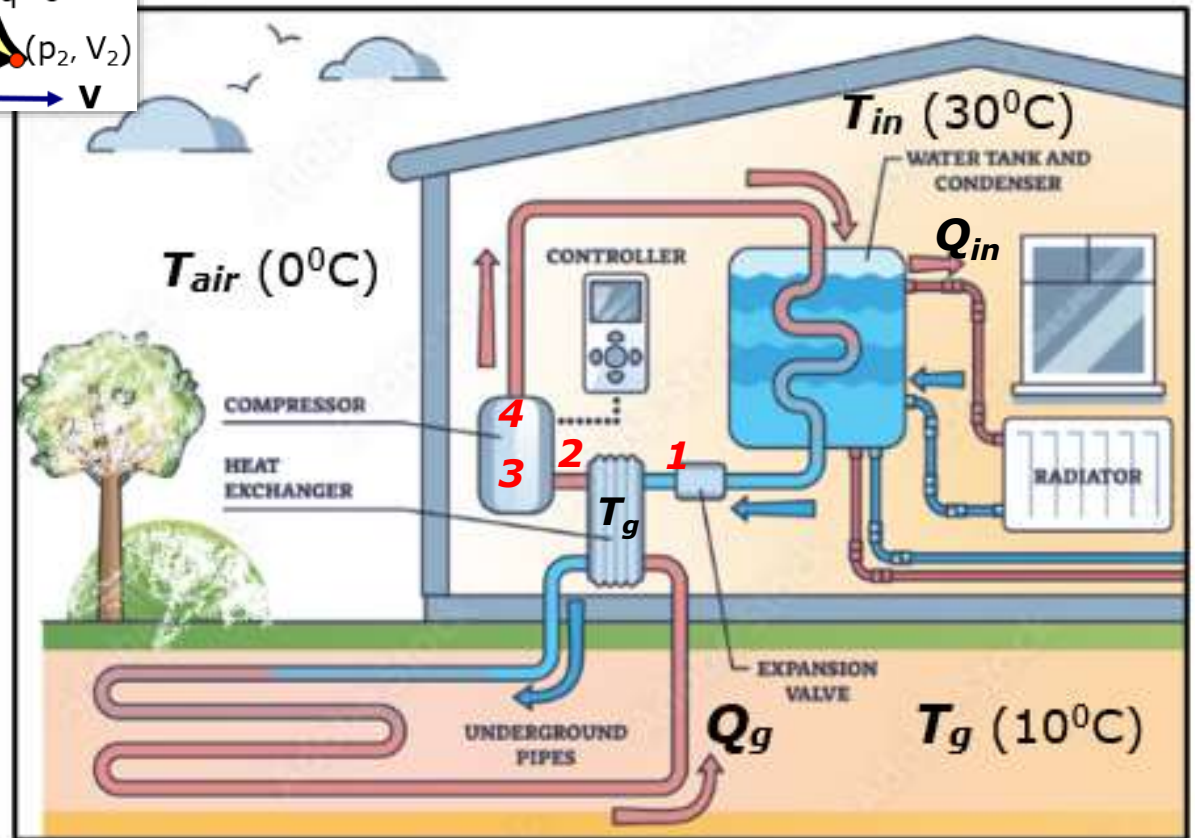


Carnot heating: In-ground heat pump absorbs heat energy  $Q_g \approx \Delta S \cdot T_g$  from under ground  $T_g$  heat bath to preheat expanded work fluid/gas. Compressor provides differential heat  $Q_{in} \approx -\Delta S \cdot T_{in}$  required for sustaining temperature  $T_{in}$ .

Work fluid transfers heat  $Q_{in} < 0$  to tank and interior. Isothermal expansion after expansion nozzle in ground loop heat exchanger.

Req. compressor work

$$w = C_{air} \cdot (T_{in} - T_{air}) - |Q_g|$$



# Thermal Power Plants



# Agenda: Thermal Power Plants

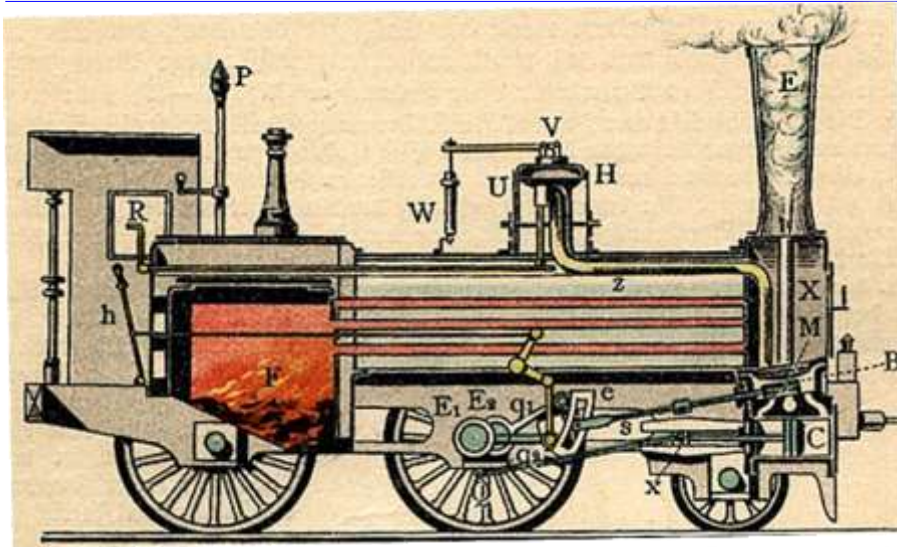
---

- Operational principle of cyclic thermodynamic engines  
Entropy, heat, and work in Carnot cycle
- Reciprocating (piston) engines  
Steam cylinder  
Otto internal combustion cycle  
Stirling engine
- Steam power plants  
Isotherms of real gases  
Steam and air as working media  
S-T cycles for Carnot, Rankine, and Brayton cycles
- Gas turbine power plants  
Combined-cycle plants
- Chemistry of complete & incomplete combustion  
Examples
- Carbon (CO<sub>2</sub>) capture processes

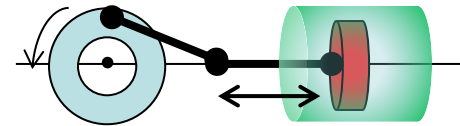
---

**Next:** Power from nuclear transmutation  
Andrew & Jelley Chs. 9 & 10

# Uniflow Steam Cylinder

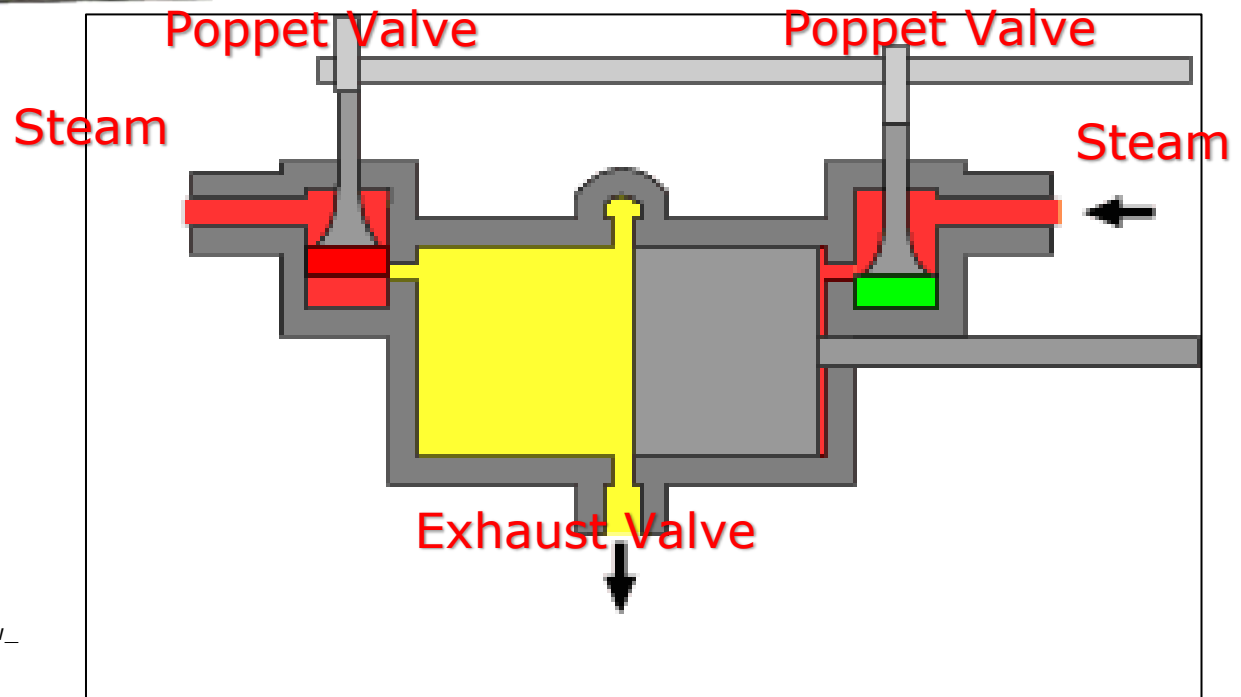


Linear motion is converted via excentric lever on crank wheel. produced by geared rotational motion, sustained by inertia.



Poppet valves connected to piston via levers or rotating crank shaft steer steam inlet and exhaust outlet.

Red = path closed  
Green = path open



[https://commons.wikimedia.org/wiki/File:Uniflow\\_steam\\_engine.gif](https://commons.wikimedia.org/wiki/File:Uniflow_steam_engine.gif)

# Early Steam Engines (America's Centennial Exposition 1876)



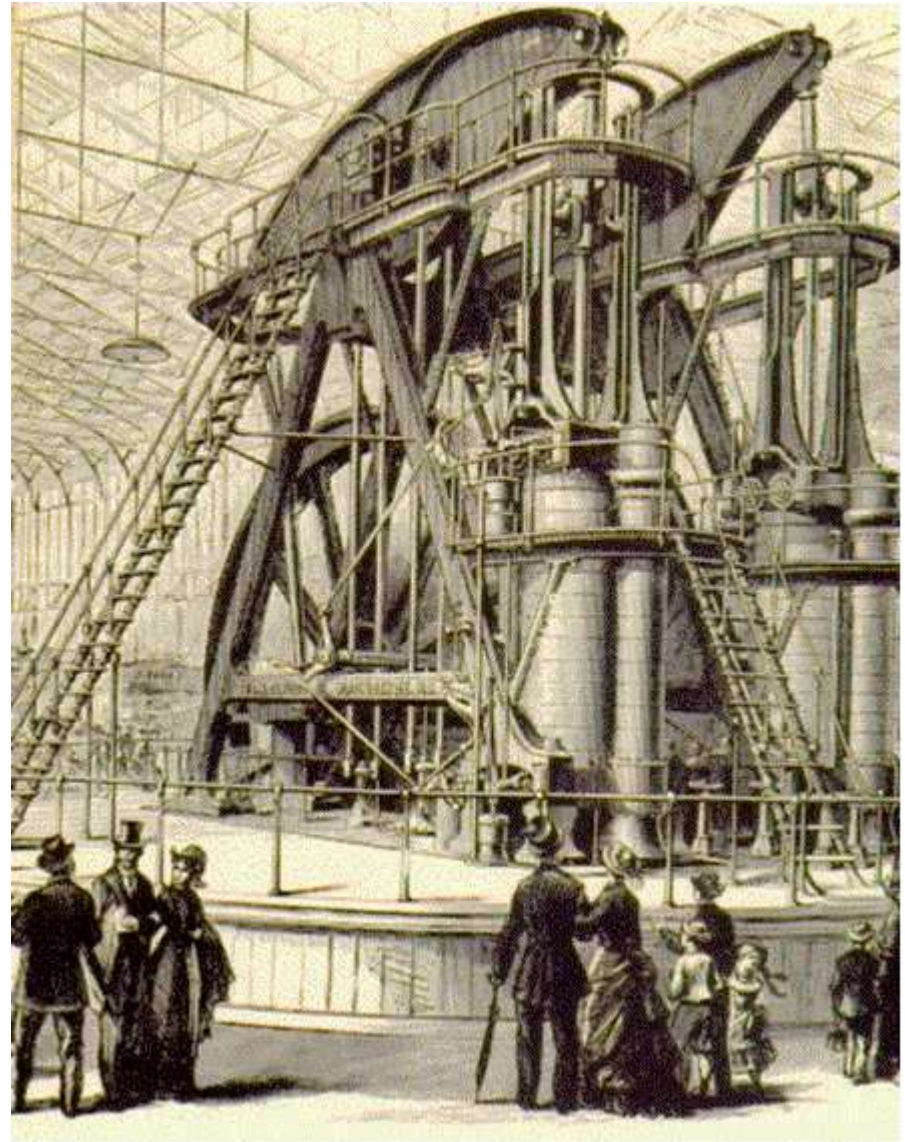
George H. Corliss.  
Inventor, Providence, RI

American made  
Corliss steam engine  
at the Philadelphia  
exhibition.

Eye witness account:  
"It stood in excess of forty-five  
feet above the floor and has  
cylinders of forty-four inches in  
diameter with a ten foot stroke.  
Another characteristic is the  
huge fifty-six ton, thirty feet in  
diameter, and twenty-four inch  
face, flywheel which made up to  
thirty-six revolutions per  
minute." (McCabe)

**America's Centennial  
Exposition, → → →  
held in Philadelphia in 1876**

The pictured steam engine  
powered all machines and devices  
in the exhibition. It was operated  
by a single engineer.  $W=1,400$  hp

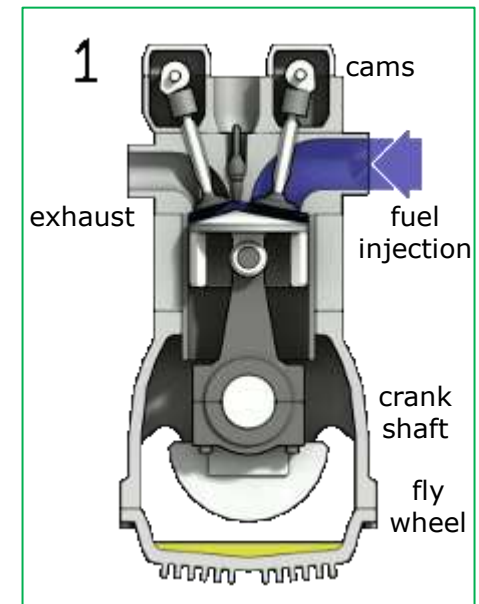
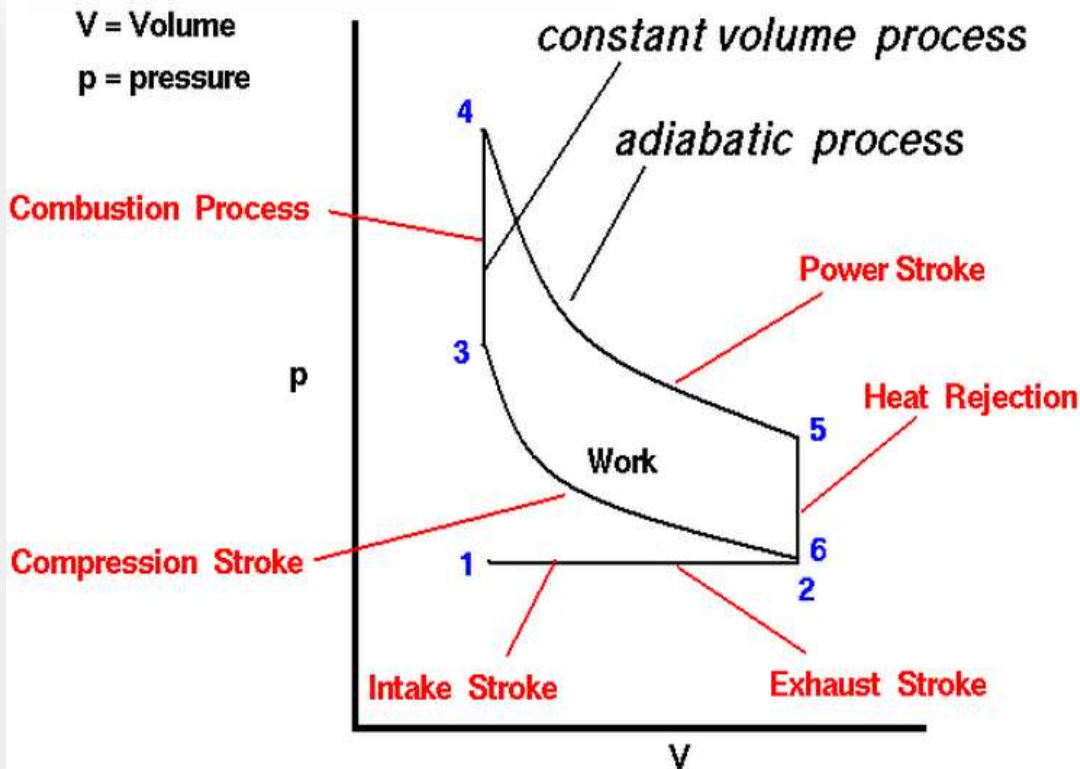


# Ideal Otto Cycle



- 1) Intake stroke (  $1 \rightarrow 2$  ), gasoline vapor and air drawn into engine.
- 2) Compression stroke (  $2 \rightarrow 3$  ) .  $p, T$  increase.
- 3) Combustion (spark) (  $3 \rightarrow 4$  ), short time,  $V = \text{constant}$ . Heat absorbed from high- $T$  "reservoir".
- 4) Power stroke: expansion (  $4 \rightarrow 5$  ).
- 5) Valve exhaust: Valve opens, gas can escape.
- 6) Emission of heat (  $5 \rightarrow 6$  ) to *low- $T$  reservoir*.
- 7) Exhaust stroke (  $6 \rightarrow 1$  ), piston evacuates cylinder.

Needs engine starter !



# Energetics of Otto Cycle

$C_v$  = Specific Heat constant volume

$\gamma$  = Specific Heat Ratio  $C_p/C_v$

$p$  = pressure

$T$  = Temperature

$V$  = Volume

$f$  = fuel / air ratio

$Q$  = Fuel heating value

$c p s$  = cycles per second

$P$  = Power

$V_2/V_3 = r$  = Compression Ratio

**Compression Stroke :**

$$T_3/T_2 = r^{\gamma-1}$$

$$p_3/p_2 = r^{\gamma}$$

**Combustion :**

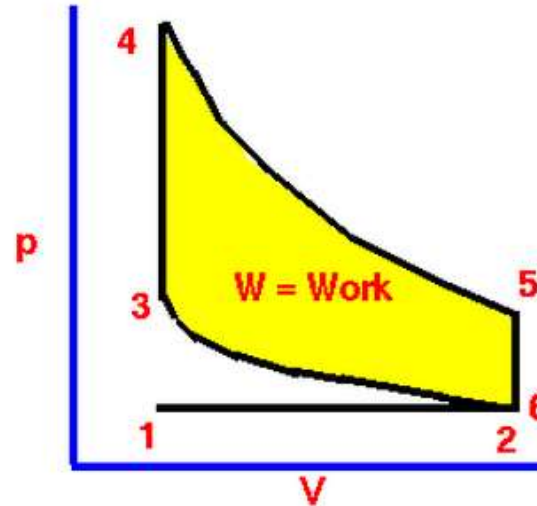
$$T_4 = T_3 + fQ/c_v$$

$$p_4 = p_3(T_4/T_3)$$

**Power Stroke :**

$$T_5/T_4 = r^{1-\gamma}$$

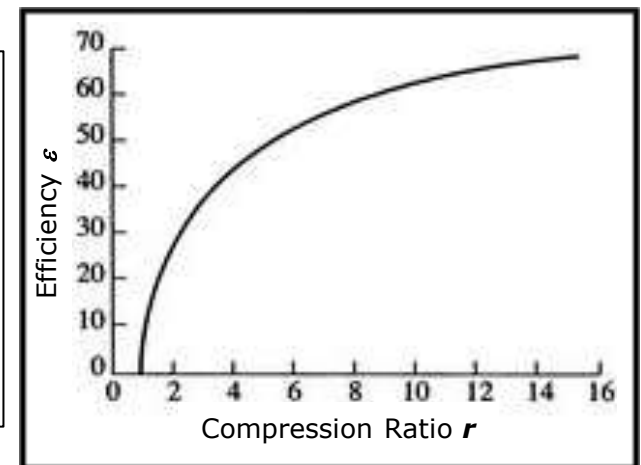
$$p_5/p_4 = r^{-\gamma}$$



$$\text{Efficiency: } \varepsilon = \frac{w}{q_{3 \rightarrow 4}} = \frac{q_{3 \rightarrow 4} + q_{5 \rightarrow 6}}{q_{3 \rightarrow 4}} = \frac{c_v(T_4 - T_3) + c_v(T_6 - T_5)}{c_v(T_4 - T_3)}$$

$$\varepsilon = 1 - \frac{(T_5 - T_6)}{(T_4 - T_3)}$$

$$\text{Adiabatic EoS } [T \cdot V^{R/c_v} = \text{const.}] \rightarrow \boxed{\varepsilon = 1 - r^{-R/c_v}}$$



# Agenda: Thermal Power Plants

---

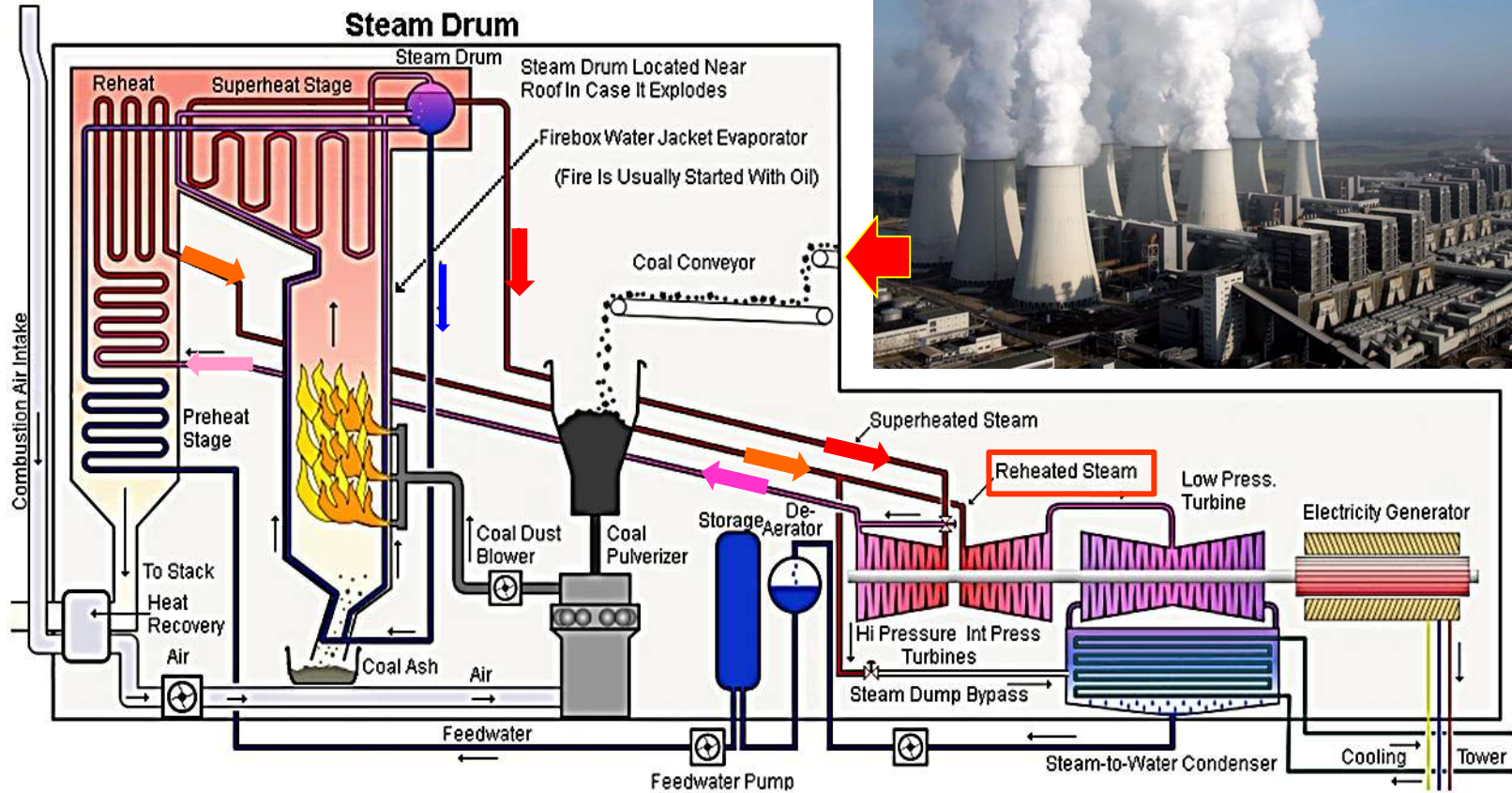
- Operational principle of cyclic thermodynamic engines  
Entropy, heat, and work in Carnot cycle
- Reciprocating (piston) engines  
Steam cylinder  
Otto internal combustion cycle  
Stirling engine
- Steam power plants  
Isotherms of real gases  
Steam and air as working media  
S-T cycles for Carnot, Rankine, and Brayton cycles
- Gas turbine power plants  
Combined-cycle plants
- Chemistry of complete & incomplete combustion  
Examples
- Carbon (CO<sub>2</sub>) capture processes

---

**Next:** Power from nuclear transmutation  
Andrew & Jelley Chs. 9 & 10

# Coal Power Plant (Photo & Schematic)

**Modern coal power plant:** 3-7 GW<sub>th</sub>.  
Two turbines in tandem working with reheated steam. Practical for  $T < 700$  °C.



# Real Substances (Different Phases: $s, \ell, g, sc$ )

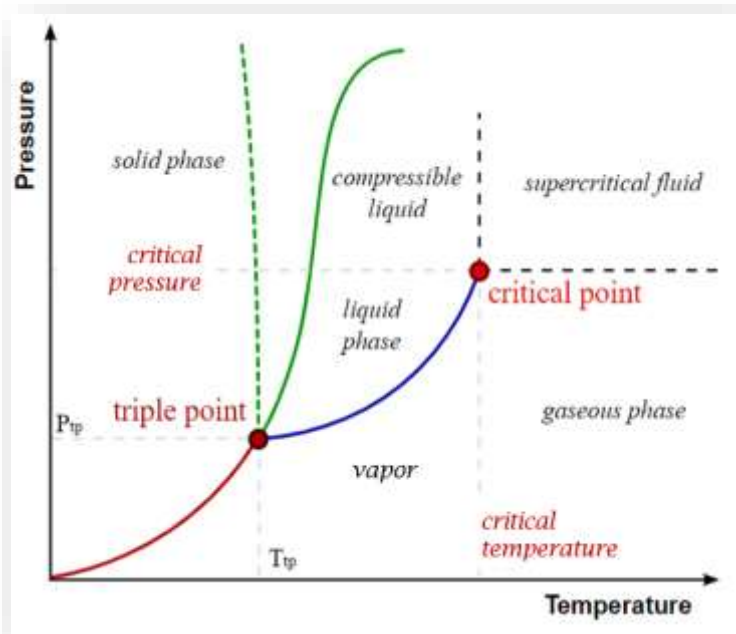
All real substances have distinct physical phases:

solid ( $T < T_{\text{freeze}}$ ), liquid ( $T_{\text{freeze}} < T < T_{\text{boil}}$ ) and gas ( $T_{\text{boil}} < T$ )

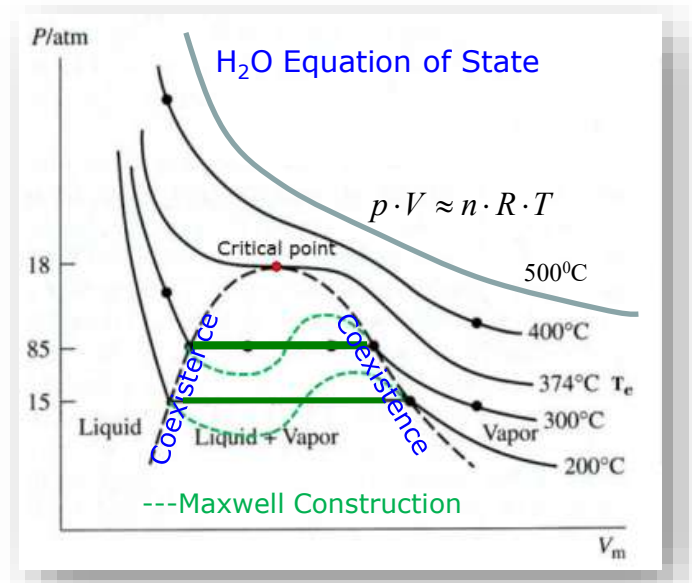
Phase transitions occur upon changes in internal energy by characteristic amounts: **latent heat** ( $\Delta$ -enthalpy) of fusion or **latent heat of vaporization**

Enthalpy  $H = U + P_{\text{ext}} \cdot V_{\text{sys}}$

at  $P_{\text{ext}} : q = \Delta H = C_p \Delta T$ ; heat capacity  $C_p$



Material	Formula	Critical pressure $P_c$		Critical temperature $T_c$		$k = C_p/C_v$
		psia	bar (abs)	$^{\circ}\text{F}$	$^{\circ}\text{C}$	
Water	$\text{H}_2\text{O}$	3206	221	705	374	1.32



--- van der Waals gas model

$$\left( p + \frac{n^2 \cdot a}{V^2} \right) \cdot (V - n \cdot b) = n \cdot R \cdot T$$

# Using Real Gases/Vapor Working Media

Since 150 years practical use: steam = water vapor, water droplets (wet steam).

→ Real gas molecules interact more, motion is less free, depending on  $\rho$ ,  $T$ .

→ **Several phases.**

Ideal – Gas EoS  $p \cdot V = R \cdot T$  (per mole) →

Virial expansion of **compression factor**

$$z = \frac{p \cdot V}{R \cdot T} = 1 + \frac{B(T)}{V} + \frac{C(T)}{V^2} + \dots =: \sum_{n=0}^{\infty} \frac{c_n(T)}{V^n}$$

## Useful Parameterizations

van der Waals EoS :

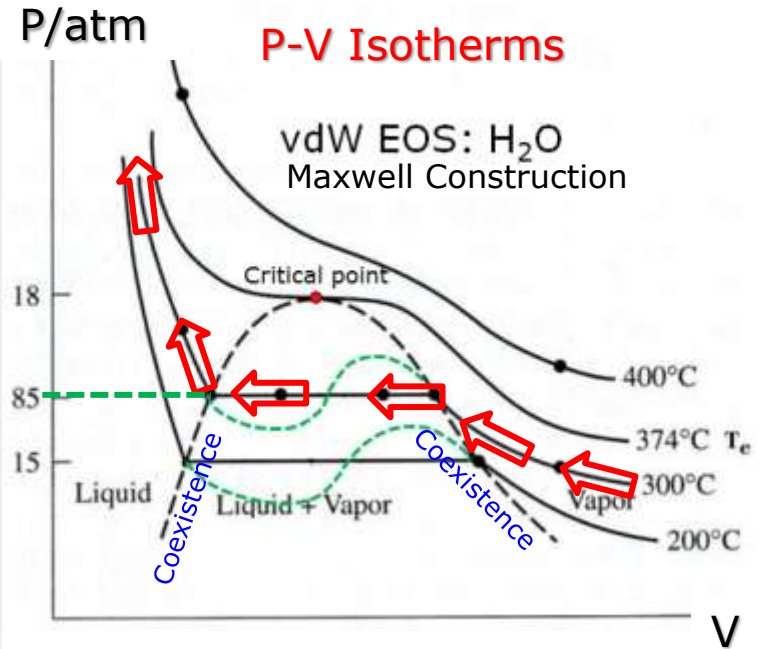
$$p = \frac{n \cdot R \cdot T}{(V - n \cdot b)} - \frac{n^2 \cdot a}{V^2}$$

Redlich Kwong EoS :

$$p = \frac{n \cdot R \cdot T}{(V - nb)} - \frac{n^2 a}{\sqrt{T}} \cdot \frac{1}{V(V + nb)}$$

## Van der Waals Parameters

Substance	a (L <sup>2</sup> atm/mol <sup>2</sup> )	b (L/mol)
He	0.0341	0.0237
H <sub>2</sub>	0.244	0.0266
O <sub>2</sub>	1.36	0.0318
H <sub>2</sub> O	5.46	0.0305
CCl <sub>4</sub>	20.4	0.1383



EoS non-monotonic → liquid-gas instability.  
High compression: real (vdW model) gases collapse (p decreases with decreasing V)  
→ **liquefaction**

Correct EoS for unphysical instability:  
**Maxwell Construction**

# Steam Tables

Absolute pressure (kPa, kN/m <sup>2</sup> )	Temperature (°C)	Specific Volume (m <sup>3</sup> /kg)	Density - ρ - (kg/m <sup>3</sup> )	Specific Enthalpy of			Specific Entropy of Steam - s - (kJ/kgK)
				Liquid - h <sub>l</sub> - (kJ/kg)	Evaporation - h <sub>e</sub> - (kJ/kg)	Steam - h <sub>s</sub> - (kJ/kg)	
0.8	3.8	160	0.00626	15.8	2493	2509	9.058
2.0	17.5	67.0	0.0149	73.5	2460	2534	8.725
5.0	32.9	28.2	0.0354	137.8	2424	2562	8.396
10.0	45.8	14.7	0.0682	191.8	2393	2585	8.151
20.0	60.1	7.65	0.131	251.5	2358	2610	7.909
28	67.5	5.58	0.179	282.7	2340	2623	7.793
35	72.7	4.53	0.221	304.3	2327	2632	7.717
45	78.7	3.58	0.279	329.6	2312	2642	7.631
55	83.7	2.96	0.338	350.6	2299	2650	7.562
65	88.0	2.53	0.395	368.6	2288	2657	7.506
75	91.8	2.22	0.450	384.5	2279	2663	7.457
85	95.2	1.97	0.507	398.6	2270	2668	7.415
95	98.2	1.78	0.563	411.5	2262	2673	7.377
100	99.6	1.69	0.590	417.5	2258	2675	7.360
<b>101.33<sup>1)</sup></b>	<b>100</b>	<b>1.67</b>	<b>0.598</b>	<b>419.1</b>	<b>2257</b>	<b>2676</b>	<b>7.355</b>
110	102.3	1.55	0.646	428.8	2251	2680	7.328
130	107.1	1.33	0.755	449.2	2238	2687	7.271
150	111.4	1.16	0.863	467.1	2226	2698	7.223
170	115.2	1.03	0.970	483.2	2216	2699	7.181
190	118.6	0.929	1.08	497.8	2206	2704	7.144
220	123.3	0.810	1.23	517.6	2193	2711	7.095
260	128.7	0.693	1.44	540.9	2177	2718	7.039
280	131.2	0.646	1.55	551.4	2170	2722	7.014
320	135.8	0.570	1.75	570.9	2157	2728	6.969

$p = 1 \text{ bar} = 101.33 \text{ kN/m}^2$

Water 0°C → 100°C.  
→ 419 kJ/kg

→ Specific enthalpy H<sub>2</sub>O:  
 $h_{\text{water}}(100^\circ\text{C}) = 419 \text{ kJ/kg}$ .

Specific enthalpy of evaporation (latent heat):  
 $h_{\text{evap}}(100^\circ\text{C}) = 2,257 \text{ kJ/kg}$

$h_{\text{steam}}(100^\circ\text{C}) = 2.676 \text{ MJ/kg}$

**Latent Heat**

# Water as a Working Power Medium

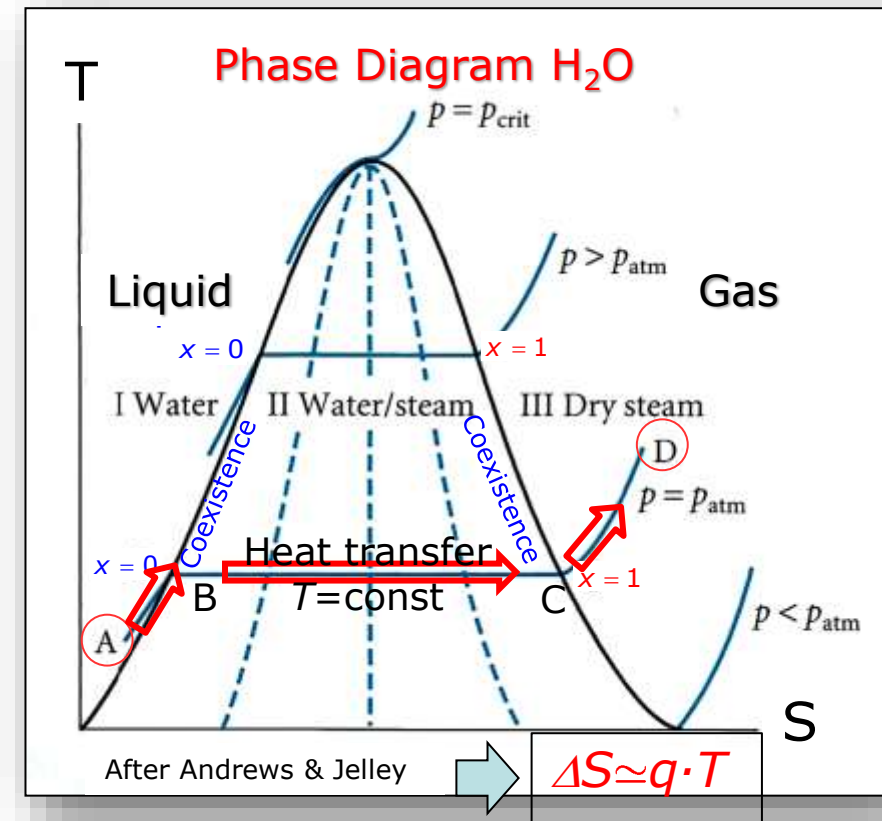
To use steam as driving gas for thermal engines, heat energy has to be transferred to water at  $T_1$  (e.g., 25°C)

- A)** heat 1mol liquid H<sub>2</sub>O to 100°C
- B-C)** evaporate all H<sub>2</sub>O (@ 100°C)
- D)** heat vapor beyond 100°C →  $T_h$

$p = 1 \text{ atm (bar)} = 101.33 \text{ kN/m}^2$   
 → Water boils @ at 100°C  
 → Need 419 kJ/kg H<sub>2</sub>O to heat water from 0°C to  $T = 100^\circ\text{C}$ .

→ @  $p = 101.33 \text{ kN/m}^2$  and 100°C  
 Specific enthalpy H<sub>2</sub>O:  
 $h_{\text{water}}(100^\circ\text{C}) = 419 \text{ kJ/kg}$ .

Specific enthalpy of evaporation (latent heat):  $h_{\text{evap}}(100^\circ\text{C}) = 2,257 \text{ kJ/kg}$   
 (not applicable to ideal gas)



Total heat required at  $p = \text{const.}$  to convert H<sub>2</sub>O to steam @ 100°C :

$$h_{\text{steam}}(100^\circ\text{C}) = (419 + 2,257) \text{ kJ/kg} = 2,676 \text{ kJ/kg} = 2.676 \text{ (MJ/kg)} = 0.74 \text{ kWh/kg}$$

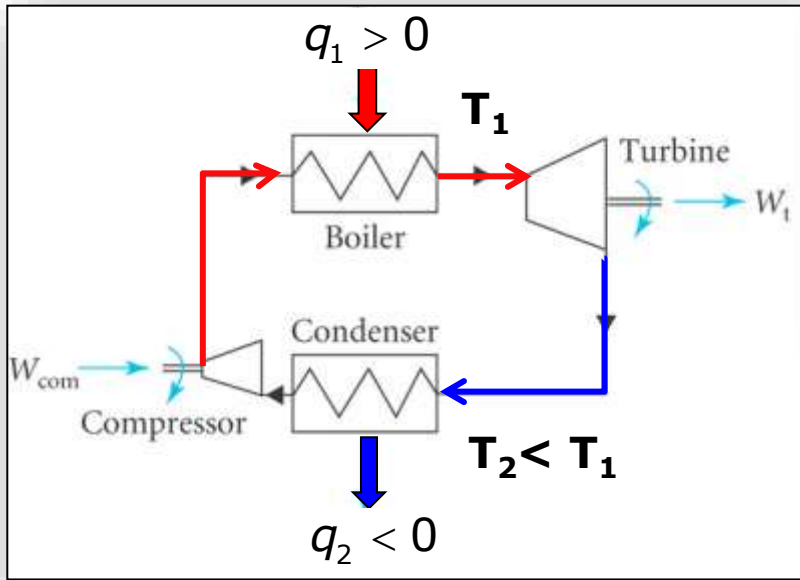
L-G mixture  $h_s(x) = (1-x) \cdot h_{\text{water}} + x \cdot h_{\text{steam}}$

Similar:  $u_s(x) = (1-x) \cdot u_{\text{water}} + x \cdot u_{\text{steam}}$

Extensive variables

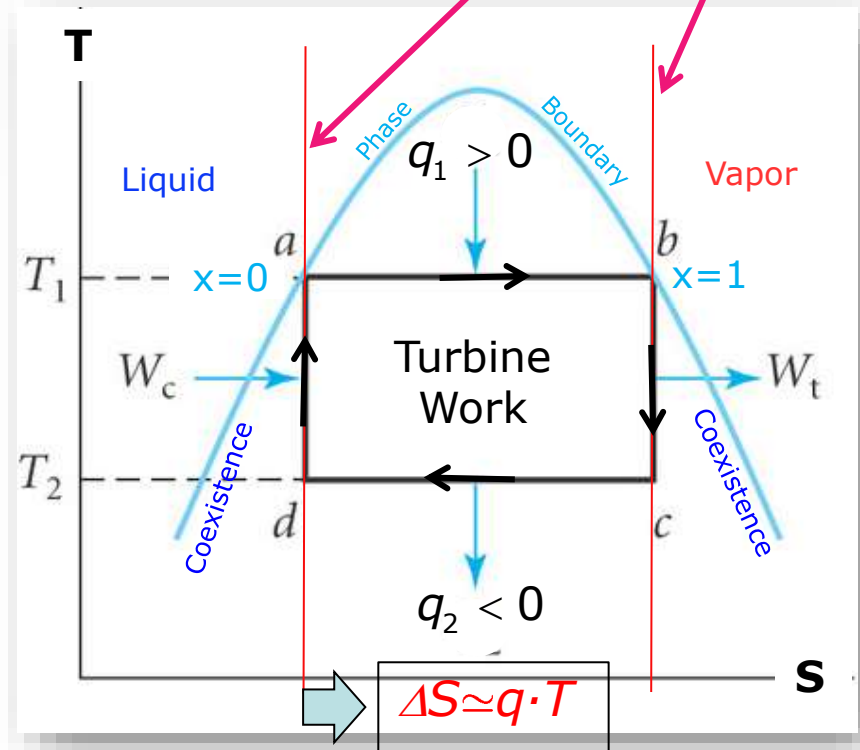
(U, H, S, ...)

# S-T Diagram for Steam Carnot Process



$T(K)$	$p$ (bar)	$h$ (kJ kg <sup>-1</sup> )		$s$ (kJ kg <sup>-1</sup> K <sup>-1</sup> )	
		$h_{fl}$	$h_{gas}$	$s_{fl}$	$s_{gas}$
303	0.04	126	2556	0.436	8.452
625	170	1690	2548	3.808	5.181

After Andrews & Jolley



Enthalpy, entropy extensive → Scale w/ x

$x = \text{steam quality}$  (fraction  $g/(g + fl)$ )

$$h = (1-x) \cdot h_{fl} + x \cdot h_{gas} \quad h = H/\text{unit mass}$$

$$s = (1-x) \cdot s_{fl} + x \cdot s_{gas} \quad s = S/\text{unit mass}$$

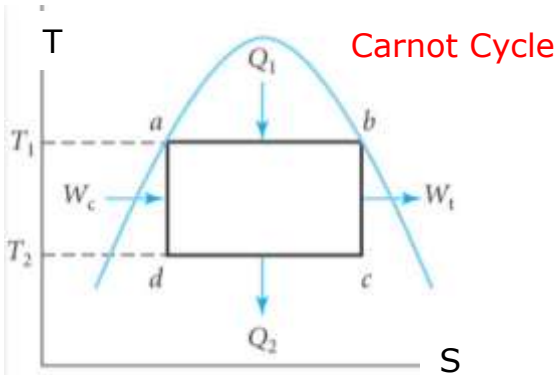
$$\text{Example: } s(d) = s(a) = 3.808 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

$$s(d) = (1-x_d) \cdot s_{fl} + x_d \cdot s_{gas} = 3.808$$

$$\quad \quad \quad 0.436 \quad \quad 8.452$$

→ Solve for  $x_d = 0.42$ , .....

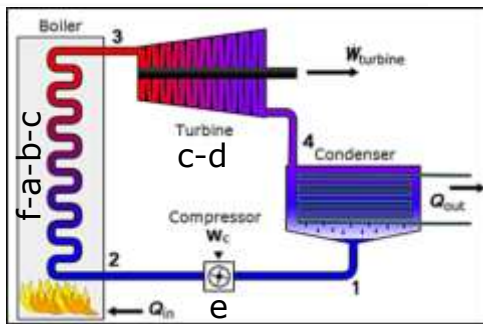
# Rankine Steam Cycle



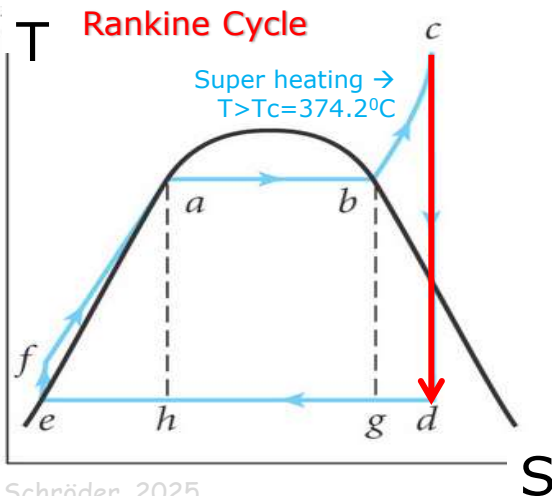
**Carnot cycle:** highest possible work output per  $q$  for  $T=\text{const.}$  processes.  
 Works well for ideal gases (simple molecules, high  $T$ )

Disadvantage for real gases and moderate  $T$ , because phase coexistence region limits gas  $T_h$  per  $q_{in}$   
 $q = T \cdot \Delta S$  in Carnot process, i.e.,  $T_h$  is limited  $\rightarrow$  low  $\epsilon$

**Rankine cycle:** (Thermodynamically robust)



$e \rightarrow f$  Compressor (pump) injects  $H_2O$  under  $p$   
 $f \rightarrow a$  Economizer heats  $H_2O$  under pressure.  
 $a \rightarrow b$  Evaporator boils  $H_2O$  under  $p = \text{const.}$   
 $b \rightarrow c$  Superheater heats steam @ high  $p = \text{const.}$   
 $c \rightarrow d$  Turbine produces work, expands steam



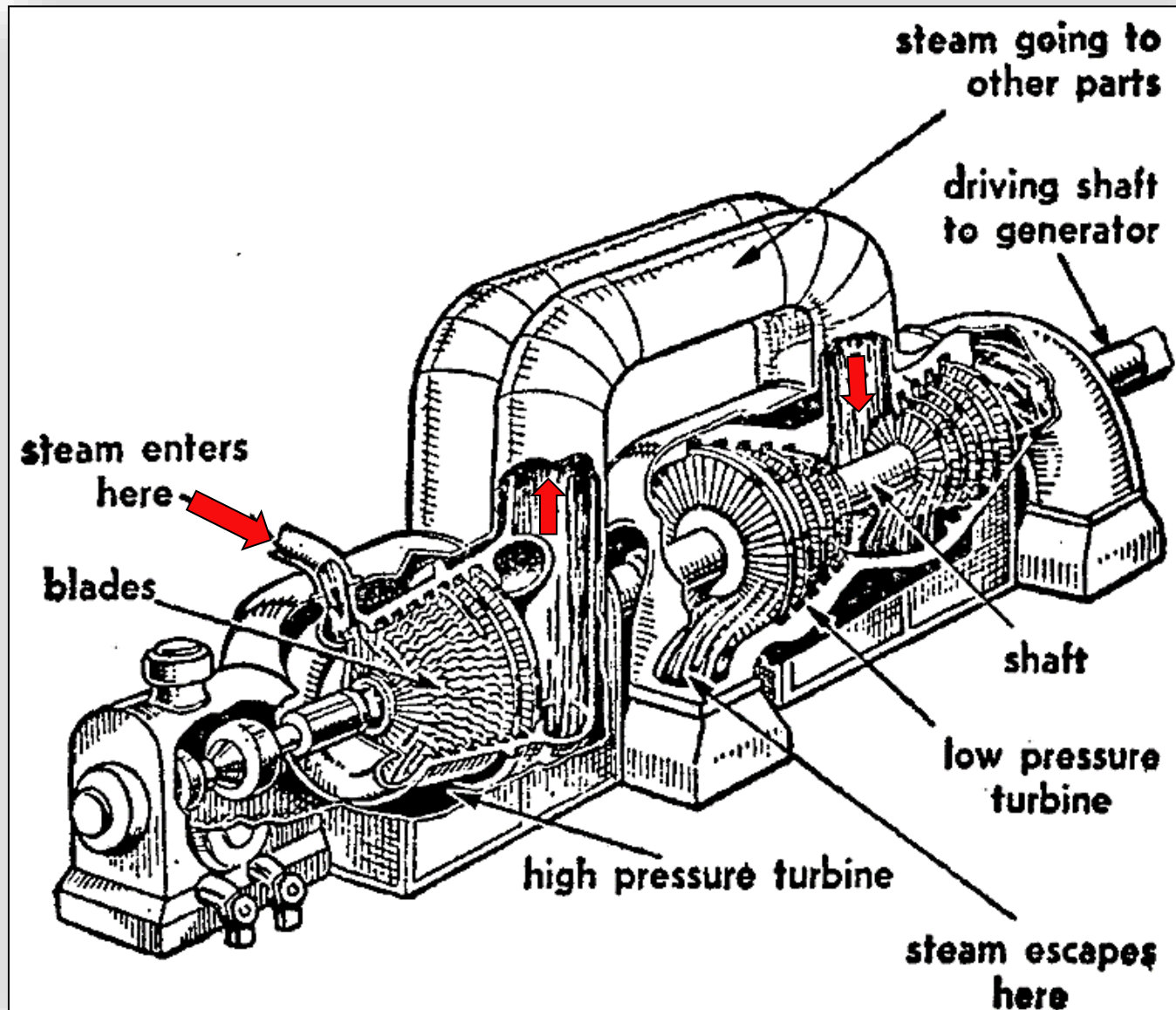
$$W_{Turbine} = H_c - H_d = \Delta(U + p \cdot V) = \int_c^d V \cdot dp \quad (S = \text{const.})$$

$d \rightarrow e$  condenser liquifies vapor @  $p < p_{at}$ .  
 Heating and cooling occur at  $p = \text{const.}$

**Efficiency:**

$$\epsilon_{Rankine} = \frac{W_{Turbine} - W_{Compressor}}{Q_{in}} = 0.3 - 0.5$$

# Low/Medium Pressure Steam Turbines



# Agenda: Thermal Power Plants

---

- Operational principle of cyclic thermodynamic engines  
Entropy, heat, and work in Carnot cycle
- Reciprocating (piston) engines  
Steam cylinder  
Stirling engine  
Otto internal combustion cycle
- Steam power plants  
Isotherms of real gases  
Steam and air as working media  
S-T cycles for Carnot, Rankine, and Brayton cycles
- Gas turbine power plants  
Gas turbine operation, enthalpy balance  
Combined-cycle plants
- Chemistry of complete & incomplete combustion  
Examples
- Carbon (CO<sub>2</sub>) capture processes

---

**Next:** Power from nuclear transmutation  
Andrew & Jelley Chs. 9 & 10