

# Lexical-Functional Grammar

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# Architecture and Structures

# Basic Syntactic Architecture of LFG

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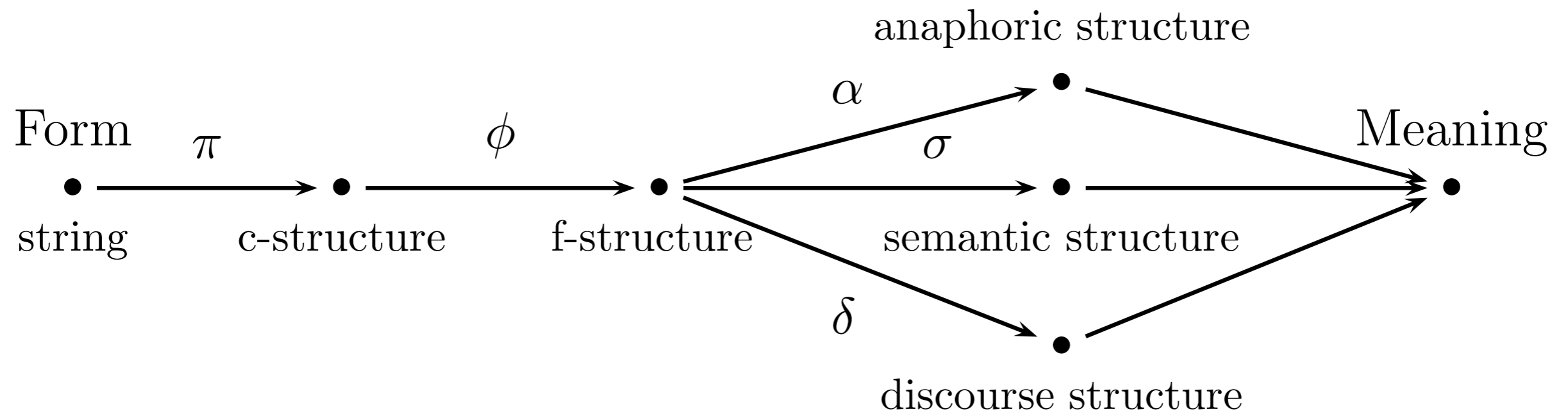
- Two basic, **simultaneous** representations of syntax:
  - **C(onstituent)-structure**: constituency, dominance, word order, phrase structure  
**Annotated trees**
  - **F(unctional)-structure**: abstract grammatical relations/functions (subject, object, etc.), tense, case, agreement, predication, local and non-local dependencies  
**Feature structures/attribute-value matrices**
- Kaplan & Bresnan (1982):

constituent structure  $\xrightarrow{\phi}$  functional structure

# LFG's Parallel Projection Architecture

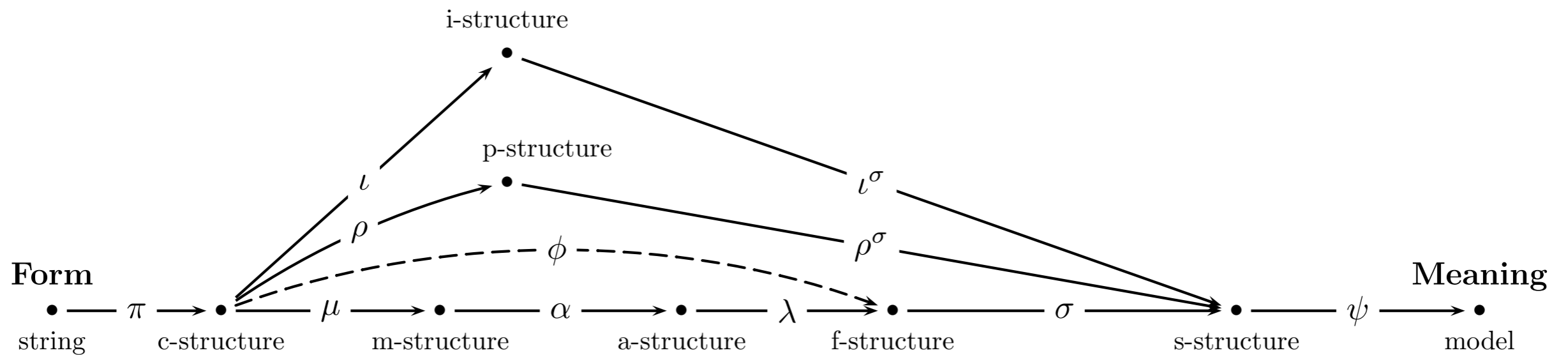
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- Kaplan (1987, 1989):



# LFG's Parallel Projection Architecture

- Asudeh (2006):



# Design Principles

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- **Principle I: Variability**

External structures (modelled by LFG **c-structures**) vary across languages.

- **Principle II: Universality**

Internal structures (modelled by LFG **f-structures**) are largely invariant across languages.

- **Principle III: Monotonicity**

The mapping from c-structure to f-structure is not one-to-one, but it is monotonic (information-preserving).

# Nonconfigurationality

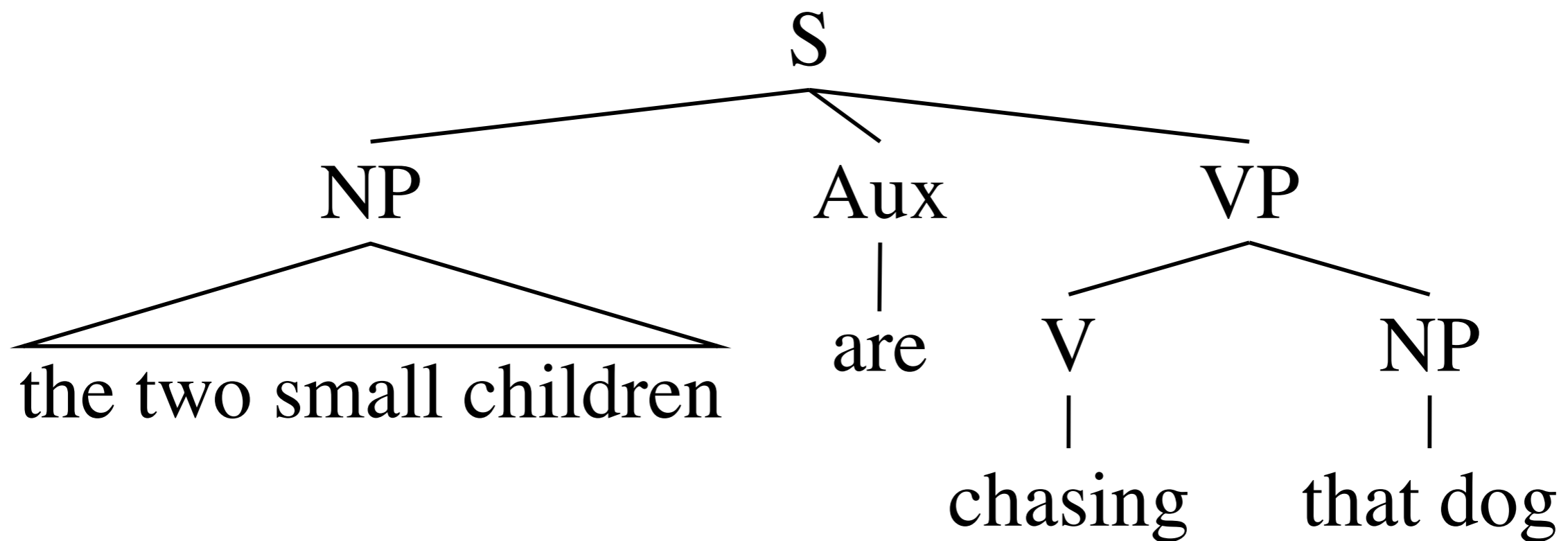
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- Two fundamental ways for language to realize underlying concepts:
  - Phrase structure (**groups**)
  - Morphology (**shapes**)
- Bresnan (1998, 2001): '**Morphology competes with syntax**'
  - English: phrase structure strategy (**configurational**)
  - Warlpiri: morphological strategy (**nonconfigurational**)

# English

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- Underlying meaning:  
That of 'the two small children are chasing that dog'





# English and Warlpiri

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- English:

- (1)
- a. The two small children are chasing that dog.
  - b. \* The two small are chasing that children dog.
  - c. \* The two small are dog chasing children that.
  - d. \* Chasing are the two small that dog children.
  - e. \* That are children chasing the two small dog.

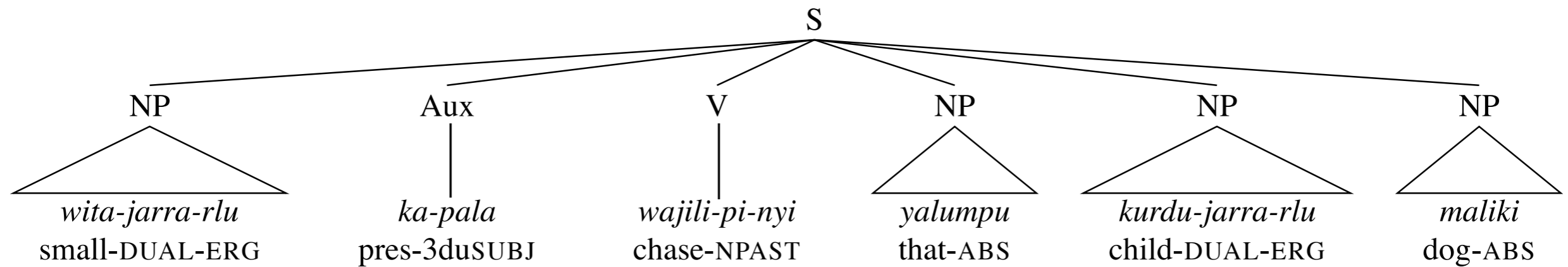
- Warlpiri:

- All of the permutations in (1) are grammatical ways to express the same underlying concept of ‘the two small children are chasing that dog’
- Even more permutations than this are possible
- Only restriction: Aux must be in second position  
(Note: this is a slight simplification)

# Warlpiri

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- Underlying meaning:  
That of 'the two small children are chasing that dog'



# Abstract Syntax

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- Despite the striking structural differences between English and Warlpiri, there are nevertheless common syntactic constraints on the two languages.

- Example: a subject can bind an object reflexive, but not vice versa

- (1) a. Lucy is hitting herself.  
b. \* Herself is hitting Lucy.

- (2) a. Napaljarri-ri            ka-nyanu            paka-rni  
    Napaljarri-ERG        PRES-REFL        hit-NONPAST  
    ‘Napaljarri is hitting herself.’

- b. \* Napaljarri            ka-nyanu paka-rni  
    Napaljarri.ABS        PRES-REFL        hit-NONPAST  
    ‘Herself is hitting Napaljarri.’

➡ How should abstract grammatical relations be captured?

**Transformational Grammar:** configurationally, using a uniform syntactic representation

**LFG:** non-configurationally, using a separate syntactic representation

# C-structure

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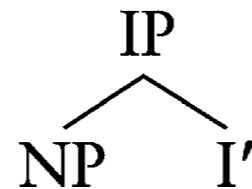
- Language variation in phrasal expression:
  - Basic word order:
    - SVO (English), SOV (Japanese), VSO (Irish), VOS (Malagasy)
  - Constituency:
    - Grouping of verb and complements,
    - Grouping of noun and modifiers
  - Strict vs. free word order:
    - configurational languages vs. case-marking languages

# Constraints on C-structures: Phrase Structure Rules

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- LFG distinguishes between the objects in the model and descriptions of those objects (i.e. **constraints** on the objects).
- C-structure trees are **constrained** by phrase structure rules.

$IP \rightarrow NP I'$



- Right-hand side of LFG phrase structure rules are **regular expressions**:

➔ disjunction, optionality, arbitrary repetition (Kleene plus [+] and star [\*])

$V' \rightarrow (V) (NP) PP^*$

# F-structures

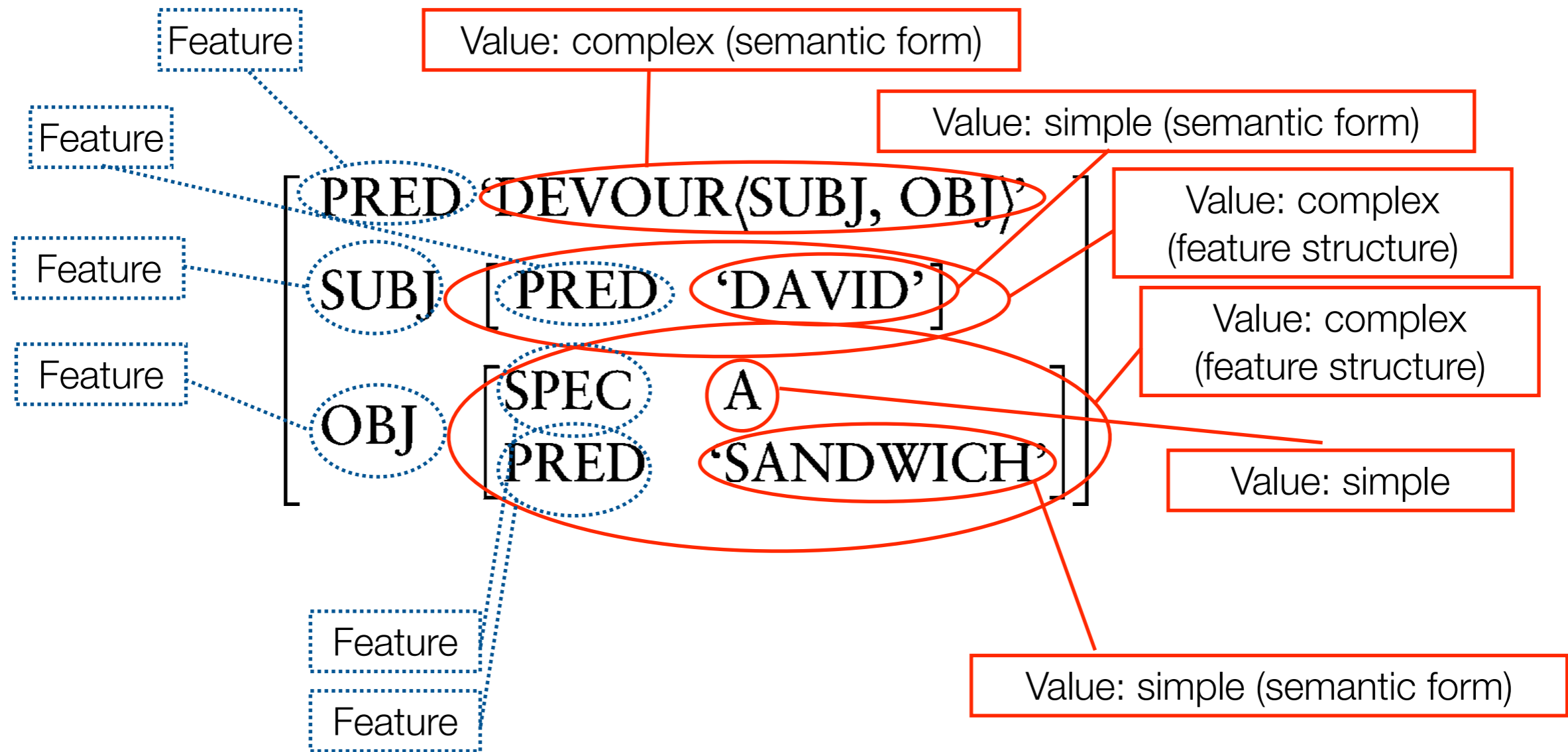
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- F-structures represent abstract **grammatical functions** (subject, object, etc.), **grammatical features** (tense, case, person, number, etc.), and **grammatical dependencies** (raising, control, unbounded dependencies)

(1) David devoured a sandwich.

$$\left[ \begin{array}{l} \text{PRED 'DEVOUR' \langle \text{SUBJ}, \text{OBJ} \rangle} \\ \text{SUBJ [ PRED 'DAVID' ]} \\ \text{OBJ [ SPEC A} \\ \quad \text{[ PRED 'SANDWICH' ]} \end{array} \right]$$

# Anatomy of an F-structure



# General Constraints on F-structures: Completeness, Coherence, Uniqueness

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- **Completeness:**

All the grammatical functions subcategorized by a predicate must be present in the f-structure.

(1)\* David devoured.

**Devour <SUBJ, OBJ>**

- **Coherence:**

Only the grammatical functions subcategorized by a predicate may be present in the f-structure.

(2)\* David devoured a sandwich that it was raining.

- **Uniqueness:**

No attribute may have more than one value.



# Uniqueness and Semantic Forms

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- Semantic forms (values of PRED features) are **unique**.

$$\left[ \begin{array}{l} \text{PRED 'DEVOUR}_{37}\langle \text{SUBJ, OBJ} \rangle \\ \text{SUBJ} \left[ \text{PRED 'DAVID}_{42}' \right] \\ \text{OBJ} \left[ \begin{array}{l} \text{SPEC A} \\ \text{PRED 'SANDWICH}_{14}' \end{array} \right] \end{array} \right]$$

➔ Multiple instances of semantic forms **cannot unify**, even if the semantic forms are otherwise compatible.

(1) \* David devoured a sandwich a sandwich.

# Features and the Lexicon in LFG

# Lexical Entries in LFG

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*yawns*

V

(↑ PRED)='yawn⟨SUBJ⟩'

(↑ VFORM)=FINITE

(↑ TENSE)=PRES

(↑ SUBJ PERS)=3

(↑ SUBJ NUM)=SG

F(unctional)-description,  
made up of functional  
schemata

# Two Main Kinds of F-structure Constraints: Defining Equations and Constraining Equations

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- Functional schemata and functional descriptions are often referred to as equations. This is a little inaccurate, because equality is not always the relevant relation, but it is certainly the most common way of specifying constraints on f-structures in LFG. So the term has stuck.
- There are two main classes of f-structure constraints in LFG:

## 1. Defining Equations

These equations define the f-structure by specifying which features have which values. They ‘make it so’. Defining equations are stated with a simple equality (or other relation symbol).

$$(f \text{ SUBJ NUM}) = \text{SG}$$

# Two Main Kinds of F-structure Constraints: Defining Equations and Constraining Equations

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- There are two main classes of f-structure constraints in LFG:

## 2. Constraining Equations

These equations further constrain the f-structure once it has been constructed.

In other words:

1. Satisfy defining equations, setting aside constraining equations, to get minimal model.
2. Satisfy constraining equations.

There are a number of different kinds of constraining equations, but the ones that check feature-value pairs are written with a subscript *c* on the equality like this:

$$(f \text{ SUBJ NUM}) =_c \text{ SG}$$

## Other Kinds of Constraining Equations

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Negative equation:  $(f \text{ TENSE}) \neq \text{PRESENT}$

Existential constraint:  $(f \text{ TENSE})$

Negative existential constraint:  $\neg(f \text{ TENSE})$

# Optionality, Disjunction, Conjunction, Negation

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sneeze     $(f \text{ PRED}) = \text{'SNEEZE<SUBJ>}'$     Conjunction (implicit)  
           $\{(f \text{ VFORM}) = \text{BASE} \mid$   
           $(f \text{ TENSE}) = \text{PRES}$     Negation  $\neg A$  or  $\neg\{ \dots \}$   
           $\neg \{(f \text{ SUBJ PERS}) = 3$   
           $(f \text{ SUBJ NUM}) = \text{SG}\}$     Disjunction  $\{ A \mid B \}$

- The lexical entry for 'sneeze' (from Dalrymple 2001:87) says the following:  
The PRED of 'sneeze' is 'SNEEZE<SUBJ>'. Also (conjunction): **Either** (disjunction) the VFORM is BASE (i.e. it's a non-finite form) **or** it has present tense and **it is not the case that** (negation) its subject has third person singular agreement features (cf. *She sneeze.*)

$((f \text{ SUBJ PRED}) = \text{'PRO'})$                       Optionality ( A )

Hint: 'pro-drop' in LFG!

# Outside-In and Inside-Out equations

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- Outside-in equations with respect to an f-structure  $f$  make specifications about paths leading **in from**  $f$ :

$$(\uparrow \text{ COMP TENSE}) = \text{PRESENT}$$

- Inside-out equations with respect to an f-structure  $f$  make specifications about paths leading **out from**  $f$ :

$$(\text{COMP } \uparrow)$$

- The two kinds of equation can be combined:

$$((\text{COMP } \uparrow) \text{ TENSE}) = \text{PRESENT}$$



# Outside-In and Inside-Out equations

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- Outside-in equations with respect to an f-structure  $f$  make specifications about paths leading **in from**  $f$ :

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- Inside-out equations with respect to an f-structure  $f$  make specifications about paths leading **out from**  $f$ :

$$(\text{COMP } f)$$

- The two kinds of equation can be combined:

$$((\text{COMP } f) \text{ TENSE}) = \text{PRESENT}$$

# Functional Uncertainty

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- Simple or limited functional uncertainty can be expressed by defining abbreviatory symbols disjunctively:

$$GF = \{ \text{SUBJ} \mid \text{OBJ} \mid \text{OBJ}_\theta \mid \text{OBL} \mid \text{COMP} \mid \text{XCOMP} \mid \text{ADJ} \mid \text{XADJ} \}$$

- Unlimited functional uncertainty can be expressed with Kleene star (\*) or Kleene plus (+), where  $X^*$  means '0 or more X' and  $X^+$  means '1 or more X':

$$(\uparrow \text{ FOCUS}) = (\uparrow \{ \text{XCOMP} \mid \text{COMP} \}^* GF)$$

$$(\uparrow \text{ INDEX}) = ((GF^+ \uparrow) \text{ SUBJ INDEX})$$

- Note that f-descriptions are therefore written in a regular language, as is also the case for the right-hand side of c-structure rules.

# Functional Descriptions and Subsumption

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- F-descriptions are true of not just the smallest, ‘intuitively intended’ f-structure, but also any larger f-structure that contains the same information.\*

\* This relationship is called **subsumption**:

In general, a structure A subsumes a structure B if and only if A and B are identical or B contains A and additional information not included in A.

$$f \left[ \begin{array}{ll} \text{PRED} & \text{'GO<SUBJ>'} \\ \text{SUBJ} & [\text{NUM} \quad \text{SG}] \end{array} \right] \quad g \left[ \begin{array}{ll} \text{PRED} & \text{'GO<SUBJ>'} \\ \text{TENSE} & \text{FUTURE} \\ \text{SUBJ} & \left[ \begin{array}{ll} \text{PRED} & \text{'PRO'} \\ \text{CASE} & \text{NOM} \\ \text{NUM} & \text{SG} \end{array} \right] \end{array} \right] \quad f \text{ subsumes } g$$

- An f-description is therefore true of not just the **minimal** f-structure that satisfies the description: the f-description is also true of the infinitely many other f-structures that the intended, minimal f-structure subsumes.

# Minimization

- There is a general requirement on LFG's solution algorithm that it yield the **minimal** solution: no features that are not mentioned in the f-description may be included.
- Let's look at an example from Dalrymple (2001).

(1) David sneezed.

- F-description:

$(f \text{ PRED}) = \text{'SNEEZE'}$   
 $(f \text{ TENSE}) = \text{PAST}$   
 $(f \text{ SUBJ}) = g$   
 $(g \text{ PRED}) = \text{'DAVID'}$

Minimal consistent f-structure

$$f: \left[ \begin{array}{ll} \text{PRED} & \text{'SNEEZE' } \langle \text{SUBJ} \rangle \\ \text{TENSE} & \text{PAST} \\ \text{SUBJ} & g: \left[ \begin{array}{ll} \text{PRED} & \text{'DAVID'} \end{array} \right] \end{array} \right]$$

Consistent but non-minimal f-structure

$$f: \left[ \begin{array}{ll} \text{PRED} & \text{'SNEEZE' } \langle \text{SUBJ} \rangle \\ \text{TENSE} & \text{PAST} \\ \text{SUBJ} & g: \left[ \begin{array}{ll} \text{PRED} & \text{'DAVID'} \\ \text{PERS} & 3 \end{array} \right] \\ \text{ADJ} & \left\{ \begin{array}{l} \left[ \begin{array}{ll} \text{PRED} & \text{'YESTERDAY'} \end{array} \right] \\ \left[ \begin{array}{ll} \text{PRED} & \text{'AT' } \langle \text{OBJ} \rangle \\ \text{OBJ} & \left[ \begin{array}{ll} \text{PRED} & \text{'NOON'} \end{array} \right] \end{array} \right] \end{array} \right\} \end{array} \right]$$

subsumes

# Lexical Generalizations in LFG

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*yawns*      V      (↑ PRED)='yawn⟨SUBJ⟩'  
(↑ VFORM)=FINITE  
(↑ TENSE)=PRES  
(↑ SUBJ PERS)=3  
(↑ SUBJ NUM)=SG

A lot of this f-description  
is shared by other verbs.

# LFG Templates: Relations between Descriptions

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*yawns*    (↑ PRED)='yawn⟨SUBJ⟩'  
              (↑ VFORM)=FINITE  
              (↑ TENSE)=PRES  
              (↑ SUBJ PERS)=3  
              (↑ SUBJ NUM)=SG

PRESENT    =    (↑ VFORM)=FINITE  
                  (↑ TENSE)=PRES  
  
3SG         =    (↑ SUBJ PERS)=3  
                  (↑ SUBJ NUM)=SG



*yawns*    (↑ PRED)='yawn⟨SUBJ⟩'  
              @PRESENT  
              @3SG

# Templates: Factorization and Hierarchies

---

FINITE = ( $\uparrow$  VFORM)=FINITE

PRES-TENSE = ( $\uparrow$  TENSE)=PRES

PRESENT = @FINITE  
@PRES-TENSE



PRES-TENSE      FINITE  
└──────────┬──────────  
          PRESENT

3PERSONSUBJ = ( $\uparrow$  SUBJ PERS)=3

SINGSUBJ = ( $\uparrow$  SUBJ NUM)=SG

3SG = @3PERSONSUBJ  
@SINGSUBJ



3PERSONSUBJ      SINGSUBJ  
└──────────┬──────────  
          3SG

# Templates: Factorization and Hierarchies

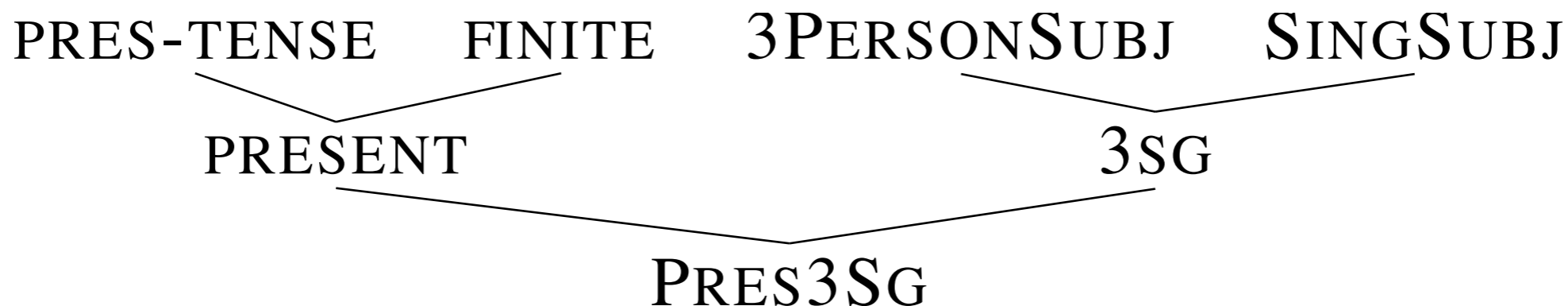
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*yawns*    (↑ PRED)='yawn⟨SUBJ⟩'  
@PRESENT  
@3SG

PRES3SG = @PRESENT  
@3SG



*yawns*    (↑ PRED)='yawn⟨SUBJ⟩'  
@PRES3SG





# Templates: Boolean Operators

PRESNOT3SG = @PRESENT  
                  ¬@3SG

Negation

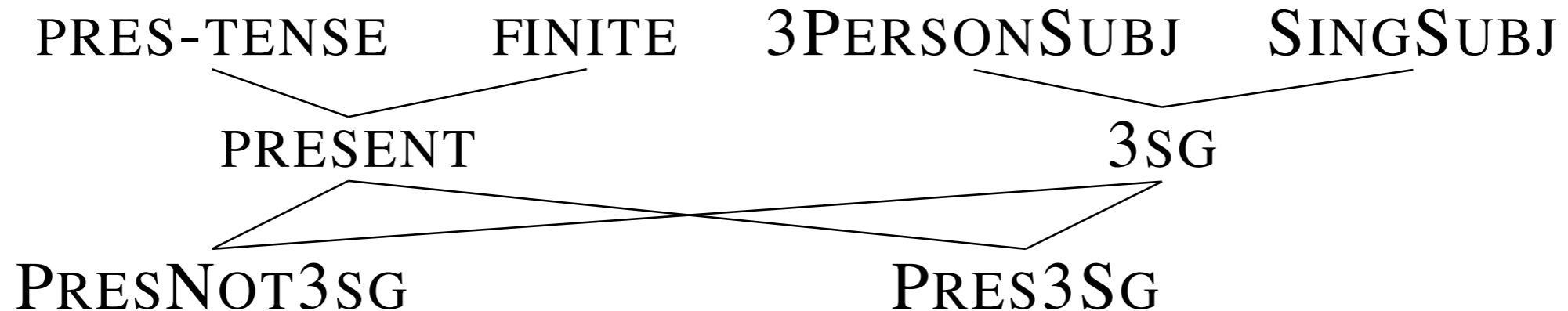


(↑ VFORM)=FINITE

(↑ TENSE)=PRES

¬{(↑ SUBJ PERS)=3

(↑ SUBJ NUM)=SG}



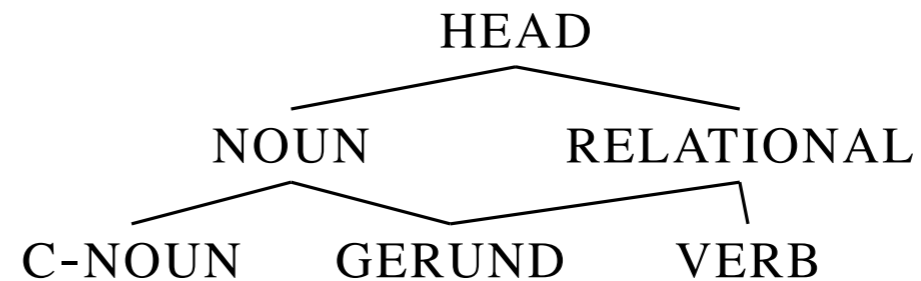
# Hierarchies: Templates vs. Types

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- Type hierarchies are *and/or* lattices:

- Motherhood: *or*

- Multiple Dominance: *and*

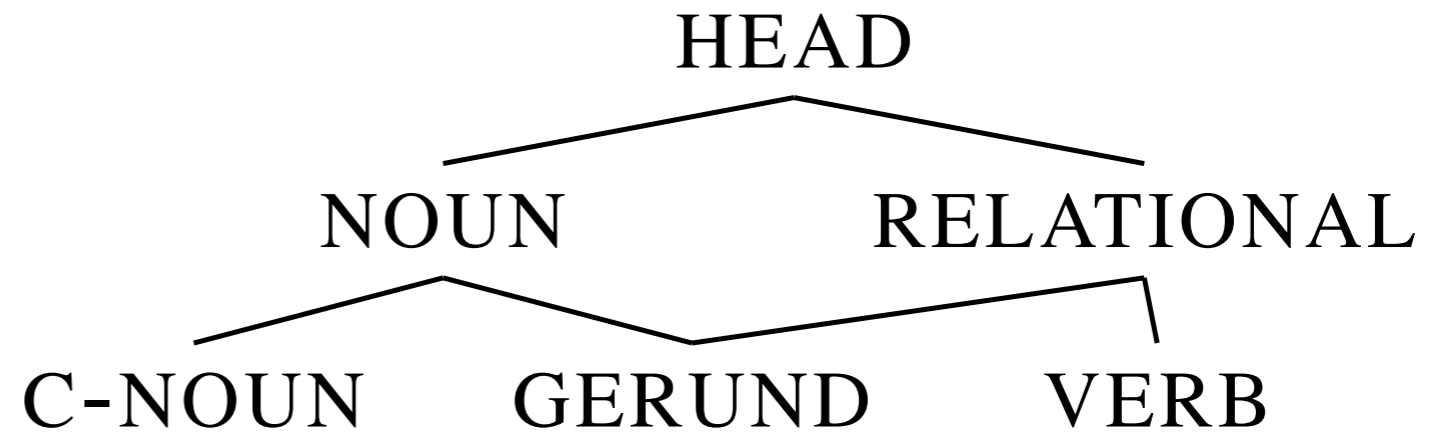


- Type hierarchies encode inclusion/inheritance and place constraints on how the inheritance is interpreted.
- LFG template hierarchies encode only inclusion: multiple dominance not interpreted as conjunction, no real status for motherhood.
- LFG hierarchies relate descriptions only: mode of combination (logical operators) is determined contextually at invocation or is built into the template.
- HPSG hierarchies relate first-class ontological objects of the theory.
- LFG hierarchies are abbreviatory only and have no real ontological status.

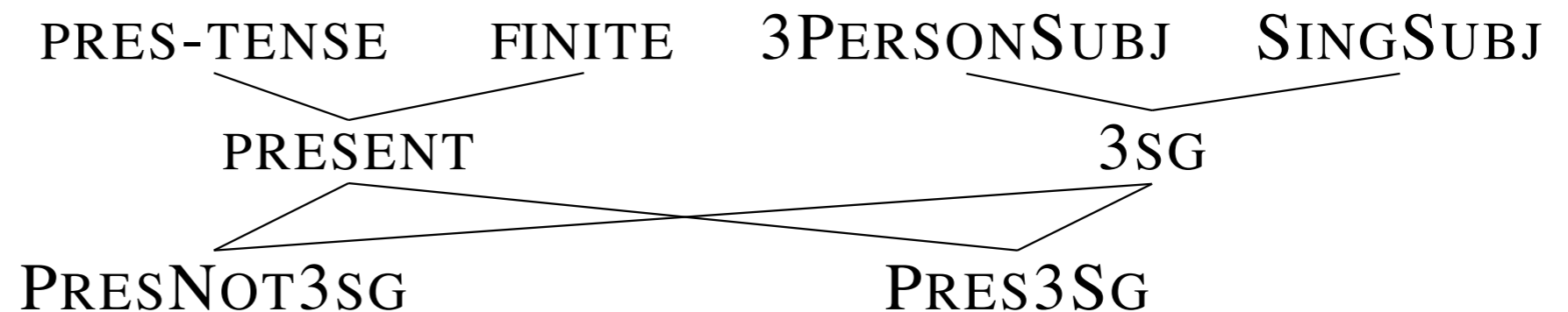
# Hierarchies: Templates vs. Types

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## HPSG



## LFG



# Parameterized Templates

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*yawns*    (↑ PRED)='yawn⟨SUBJ⟩'    INTRANSITIVE(P) = (↑ PRED)='P⟨SUBJ⟩'  
          @PRES3SG



*yawns*    @INTRANSITIVE(yawn)  
          @PRES3SG

# Parameterized Templates

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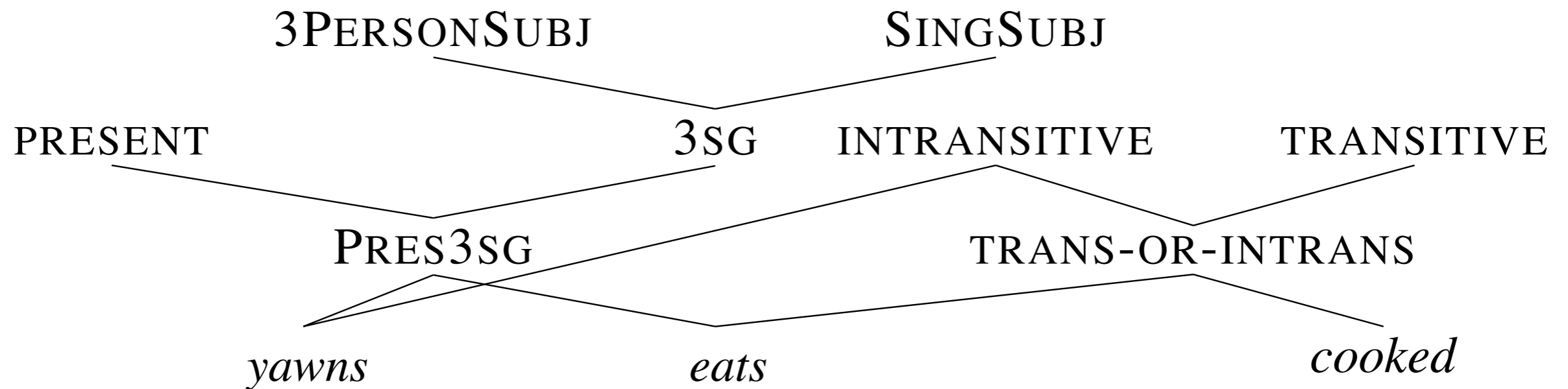
TRANSITIVE(P) = ( $\uparrow$  PRED)=‘P⟨SUBJ, OBJ⟩’

TRANS-OR-INTRANS(P) = @TRANSITIVE(P)  $\vee$  @INTRANSITIVE(P)

( $\uparrow$  PRED)=‘*eat*⟨SUBJ, OBJ⟩’  $\vee$  ( $\uparrow$  PRED)=‘*eat*⟨SUBJ⟩’

# Temple Hierarchy with Lexical Leaves

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# Defaults in LFG

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$(\uparrow \text{ CASE}) \vee (\uparrow \text{ CASE})=\text{NOM}$

The f-structure must have case and if nothing else provides its case, then its case is nominative.

$\text{DEFAULT}(\text{D } \vee) = \text{D } \vee \text{D}=\text{V}$

Parameterized template for defaults.

Also illustrates that parameterized templates can have multiple arguments



$@\text{DEFAULT}((\uparrow \text{ CASE}) \text{ NOM})$

# C-structure Annotation of Templates

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$VP \longrightarrow V \quad ADVP^*$   
 $\uparrow = \downarrow \quad \downarrow \in (\uparrow \text{ADJUNCT})$   
 $(\downarrow \text{ADJUNCT-TYPE}) = VP-ADJ$

$\text{ADJUNCT}(P) = \downarrow \in (\uparrow \text{ADJUNCT})$   
 $\quad \quad \quad @\text{ADJUNCT-TYPE}(P)$

$\text{ADJUNCT-TYPE}(P) = (\downarrow \text{ADJUNCT-TYPE}) = P$



$VP \longrightarrow V \quad ADVP^*$   
 $\uparrow = \downarrow \quad @\text{ADJUNCT}(VP-ADJ)$



# Features in the Minimalist Program

# Features and Explanation

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- The sorts of features that are associated with functional heads in the Minimalist Program are well-motivated morphosyntactically, although other theories may not draw the conclusion that this merits phrase structural representation (cf. Blevins 2008).
- Care must be taken to avoid circular reasoning in feature theory:
  - The ‘strong’ meta-feature: “This thing has whatever property makes things displace, as evidenced by its displacement.”
  - The ‘weak’ meta-feature: “This thing lacks whatever property makes things displace, as evidenced by its lack of displacement.”
  - The EPP feature: “This thing has whatever property makes things move to subject position, as evidenced by its occupying subject position.”

# Features and Simplicity

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- Adger (2003, 2008) considers three kinds of basic features:
  - Privative, e.g. [singular]
  - Binary, e.g. [singular +]
  - Valued, e.g. [number singular]
- Adger considers the privative kind the simplest in its own right.
- This may be true, but only if it does not introduce complexity elsewhere in the system (Culicover & Jackendoff 2005: ‘honest accounting’).
- Notice that only the final type of feature treats number features as any kind of natural class within the theory (as opposed to meta-theoretically).

# Kinds of Feature-Value Combinations

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- Adger (2003):
  - Privative
    - [singular], [M], ...
  - Binary
    - [singular: +] (?)
  - Attribute-value
    - [Tense: past]

# Interpreted vs. Uninterpreted Features

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- Interpreted features:
  - [F]
- Uninterpreted features:
  - [*u*F]
- All uninterpreted features must be eliminated ('checked').
- Interpreted features are interpreted by the semantics.
  - Presupposes an interpretive (non-combinatorial) semantics.

[Notation from Adger 2003]

# Feature Strength

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- Strong features must be checked locally:  
Trigger Move/Internal Merge/Remerge
  - [F\*]
- Weak features do not have to be checked locally:  
Do not trigger Move
  - [F]

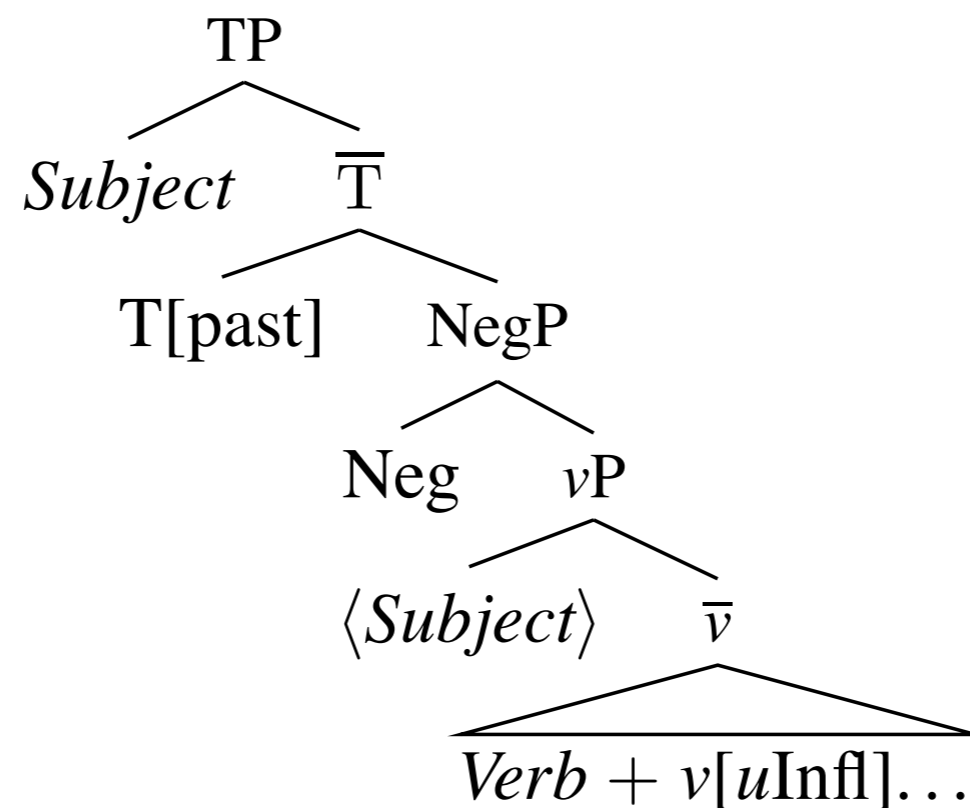
[Notation from Adger 2003]

# An Example: Auxiliaries

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- Adger (2003:181)

“When [*uInfl*: ] on Aux is valued by T, the value is strong;  
when [*uInfl*: ] on *v* is valued by T, the value is weak.”



# Locality of Feature Matching

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- Adger (2003:218)

## **Locality of Matching**

Agree holds between a feature  $F$  on  $X$  and a matching feature  $F$  on  $Y$  if and only if there is no intervening  $Z[F]$ .

## **Intervention**

In a structure  $[X \dots Z \dots Y]$ ,  $Z$  intervenes between  $X$  and  $Y$  iff  $X$  c-commands  $Z$  and  $Z$  c-commands  $Y$ .



# Feature-Value Unrestrictiveness & Free Valuation

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- Asudeh & Toivonen (2006) argue that the Minimalist feature system of Adger (2003) has two undesirable properties.

## **Feature-value unrestrictiveness**

Feature valuation is unrestricted with respect to what values a valued feature may receive.

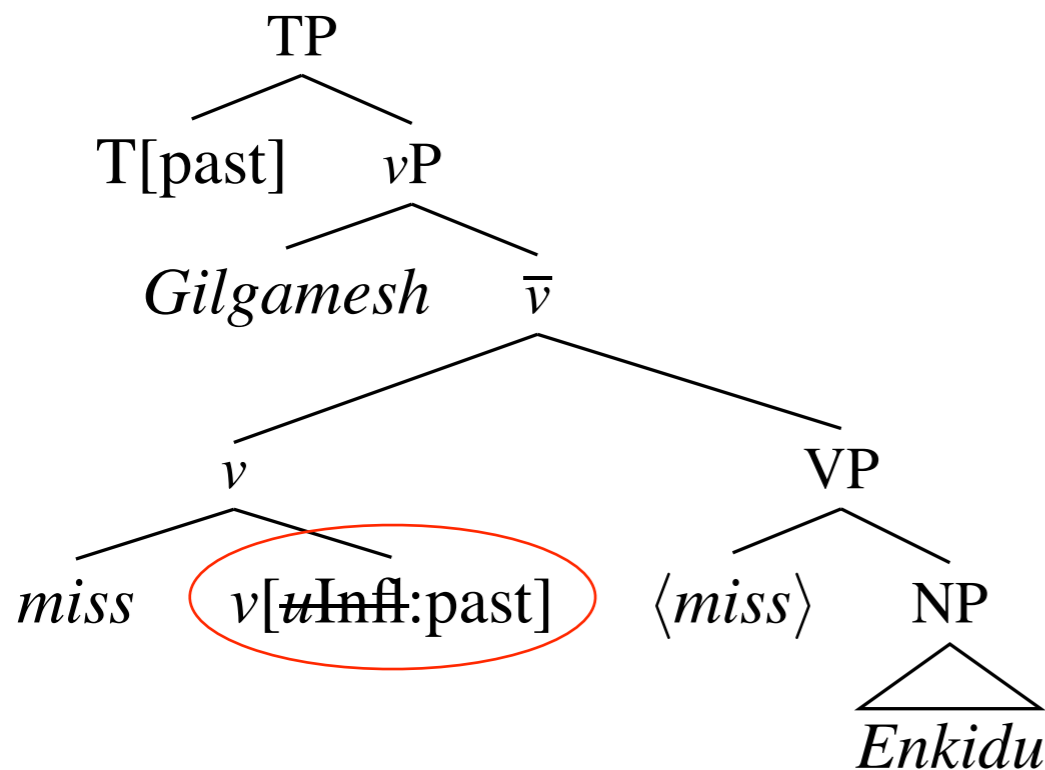
## **Free valuation**

Feature valuation appears freely, subject to locality conditions.

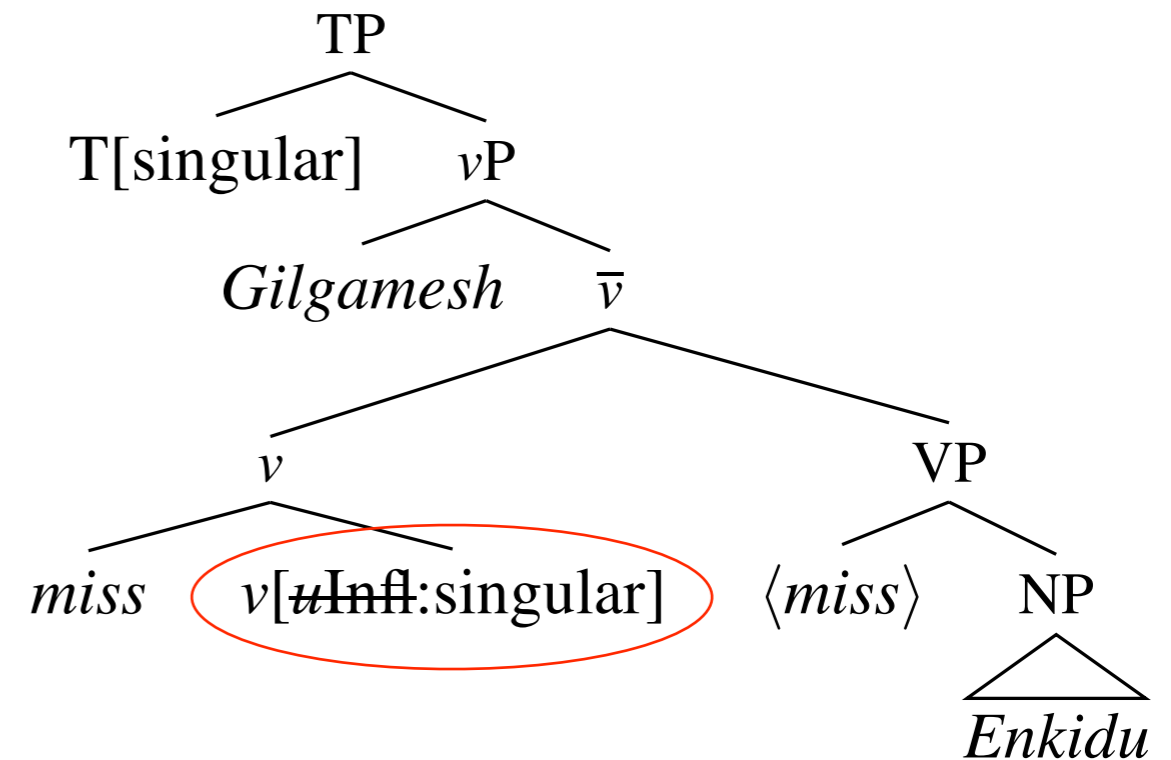
- This results in a very unconstrained theory of features.
- This may sound good, because it's less stipulative and hence more Minimal, but from a theory perspective it is bad: unconstrained theories are less predictive.

# Example: English Subject Agreement

(1) Gilgamesh missed Enkidu



(2) Gilgamesh misses Enkidu



- Contrast with HPSG: MP has no typing of values (feature value unrestrictiveness)
- Contrast with LFG: MP has valuation without specification (free valuation)

# Two Contrasting Feature Theories

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- HPSG (Pollard & Sag 1994): features are not just valued, the values are also *typed*
  - If two values can unify, they must be in a typing relation (one must be a subtype of the other).
  - Feature values in HPSG are thus tightly restricted by types.
- LFG (Kaplan & Bresnan 1982, Bresnan 2001): features are not restricted, but there is no free valuation
  - A feature cannot end up with a given value unless there is an explicit equation in the system.

# Feature Simplicity and Constraint Types

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- LFG offers the opportunity to consider Adger's three feature types in light of a single feature type, with varying constraint types.

- LFG features are valued ( $f$  is an LFG f(unctional)-structure):

$$f \left[ \text{NUMBER} \quad \text{singular} \right]$$

- Types of LFG feature constraints.

- Defining equation:  $(f \text{ NUMBER}) = \text{singular}$

- Existential constraint:  $(f \text{ NUMBER})$

- Negative existential constraint:  $\neg(f \text{ NUMBER})$

- Constraining equation:  $(f \text{ NUMBER}) =_c \text{singular}$

- Negative constraining equation:  $(f \text{ NUMBER}) \neq \text{singular}$

# Feature Simplicity and Constraint Types

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- All features treated as valued features: no restriction on constraint types
- All features treated as binary features: only positive and negative constraining equations allowed
- All features treated as privative: only negative and existential constraints allowed
  - This understanding of privative features actually does treat number as a natural class.
- This treats the notion of feature simplicity as a kind of meta-theoretical statement in an explicit, non-ad-hoc feature theory.

# Control and Raising

# Lexical Entries

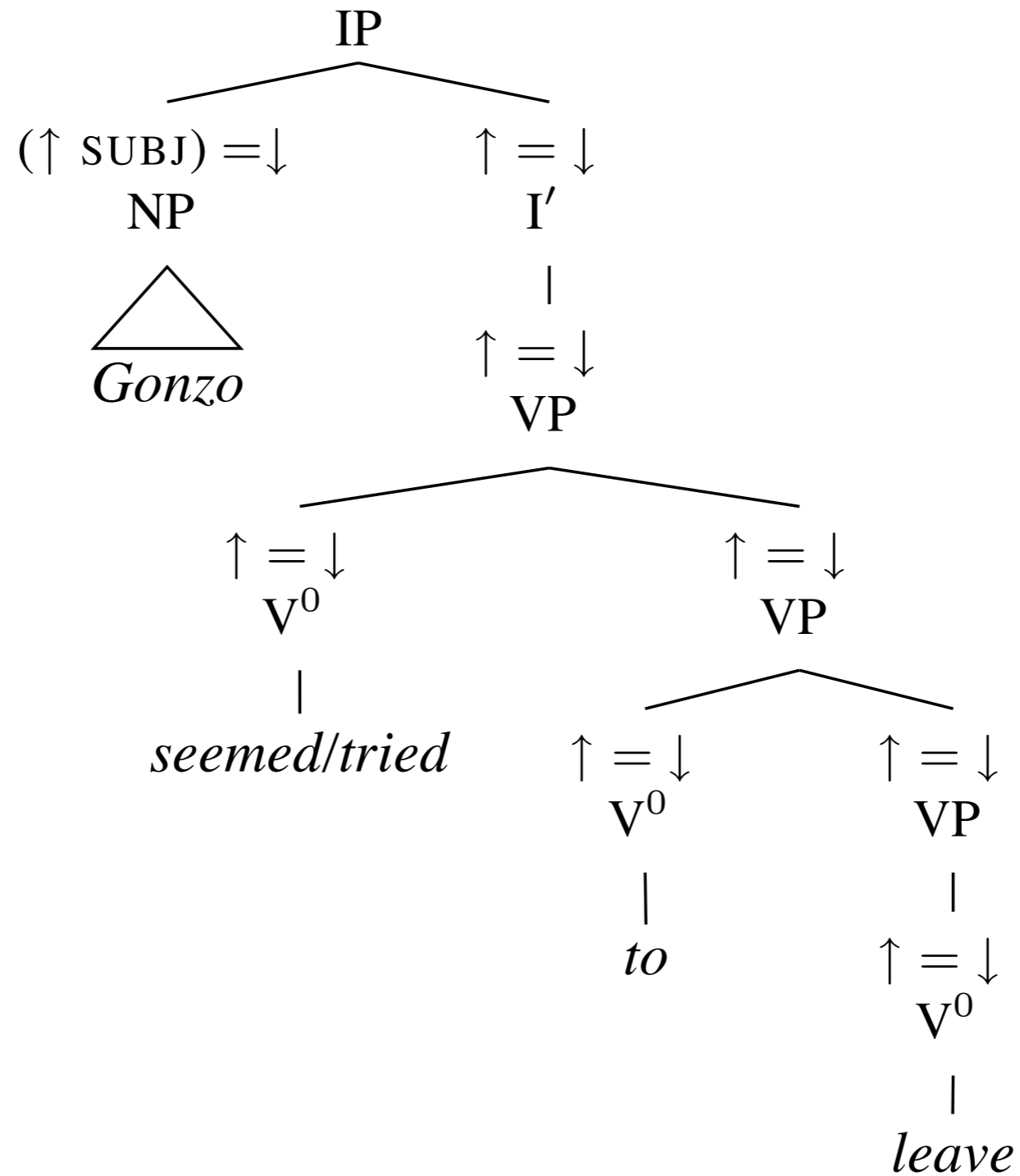
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*tried*    V    ( $\uparrow$  PRED) = 'try<SUBJ, XCOMP>'  
( $\uparrow$  SUBJ) = ( $\uparrow$  XCOMP SUBJ)

*seemed*    V    ( $\uparrow$  PRED) = 'seem<CF>SUBJ'  
{ ( $\uparrow$  SUBJ) = ( $\uparrow$  XCOMP SUBJ) |  
  ( $\uparrow$  SUBJ PRONTYPE) = EXPLETIVE  
  ( $\uparrow$  SUBJ FORM) = IT  
  ( $\uparrow$  COMP) }

# Raising to Subject/Subject Control C-structure

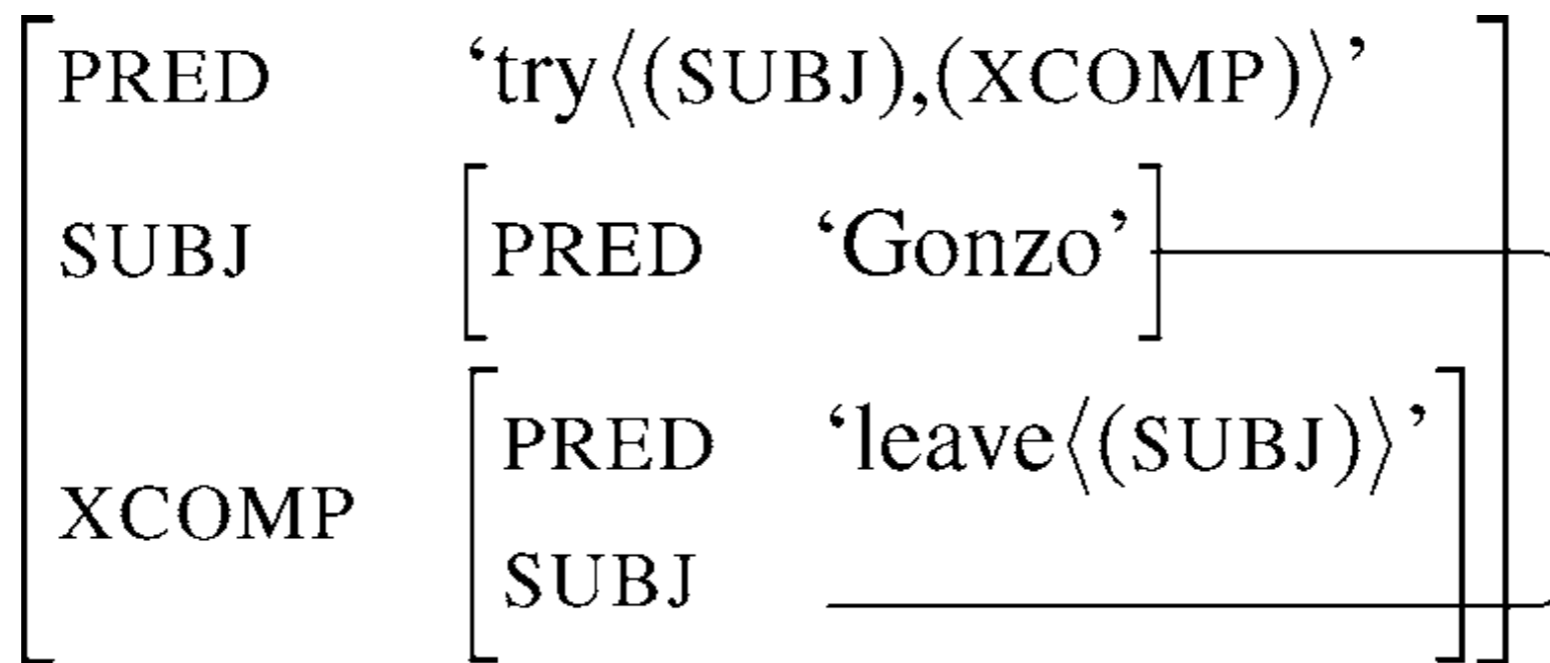
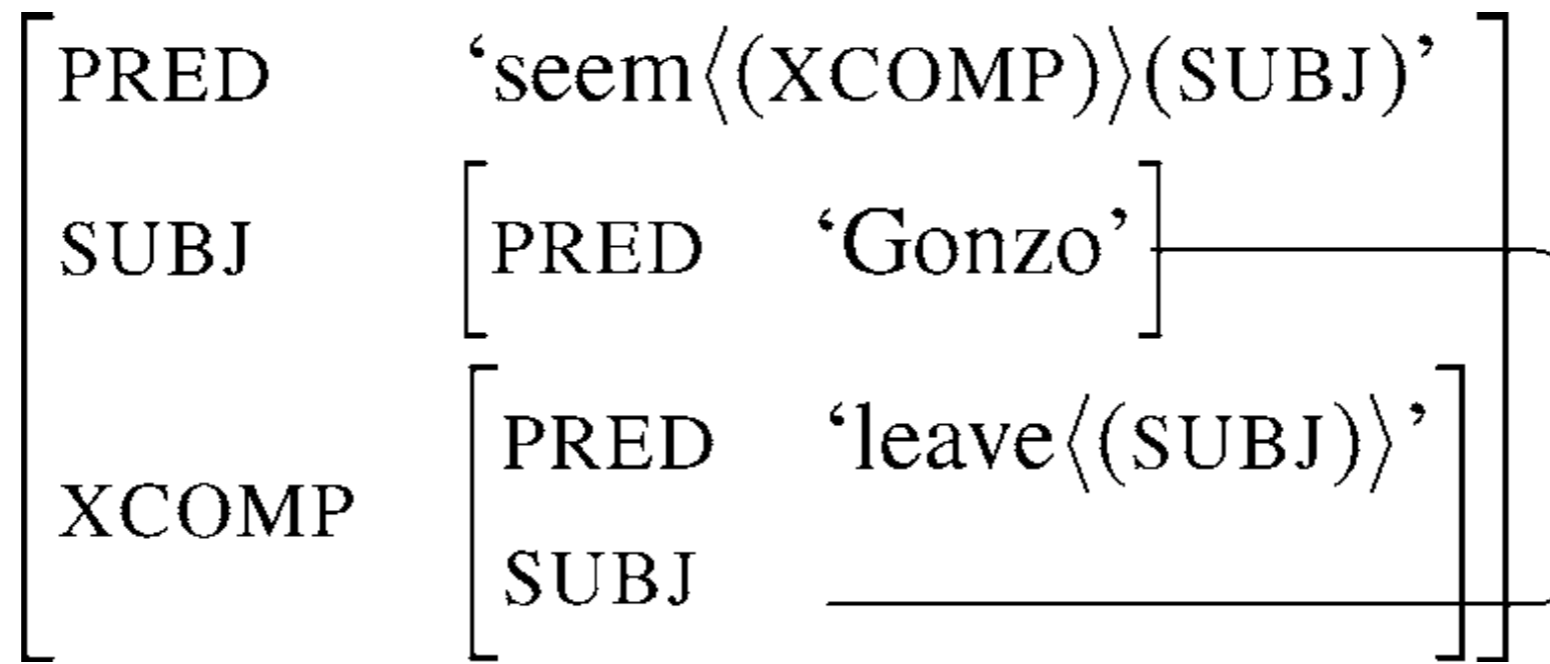
---





# F-structures

---



# Copy Raising

# Data

---

- (1) Thora seems like she enjoys hot chocolate.
- (2) Thora seems like Isak pinched her again.
- (3) Thora seems like Isak ruined her book.
- (4)\* Thora seems like Isak enjoys hot chocolate.
- (5)\* Thora seems like Isak pinched Justin again.
- (6)\* Thora seems like Isak ruined Justin's book.

# Data

---

(7) It seems like there is a problem here.

(8) It seems like Thora is upset.

(9) It seems like it rained last night.

(10) There seems like there's a problem here.

(11) \* There seems like it rained last night.

# Lexical Entries

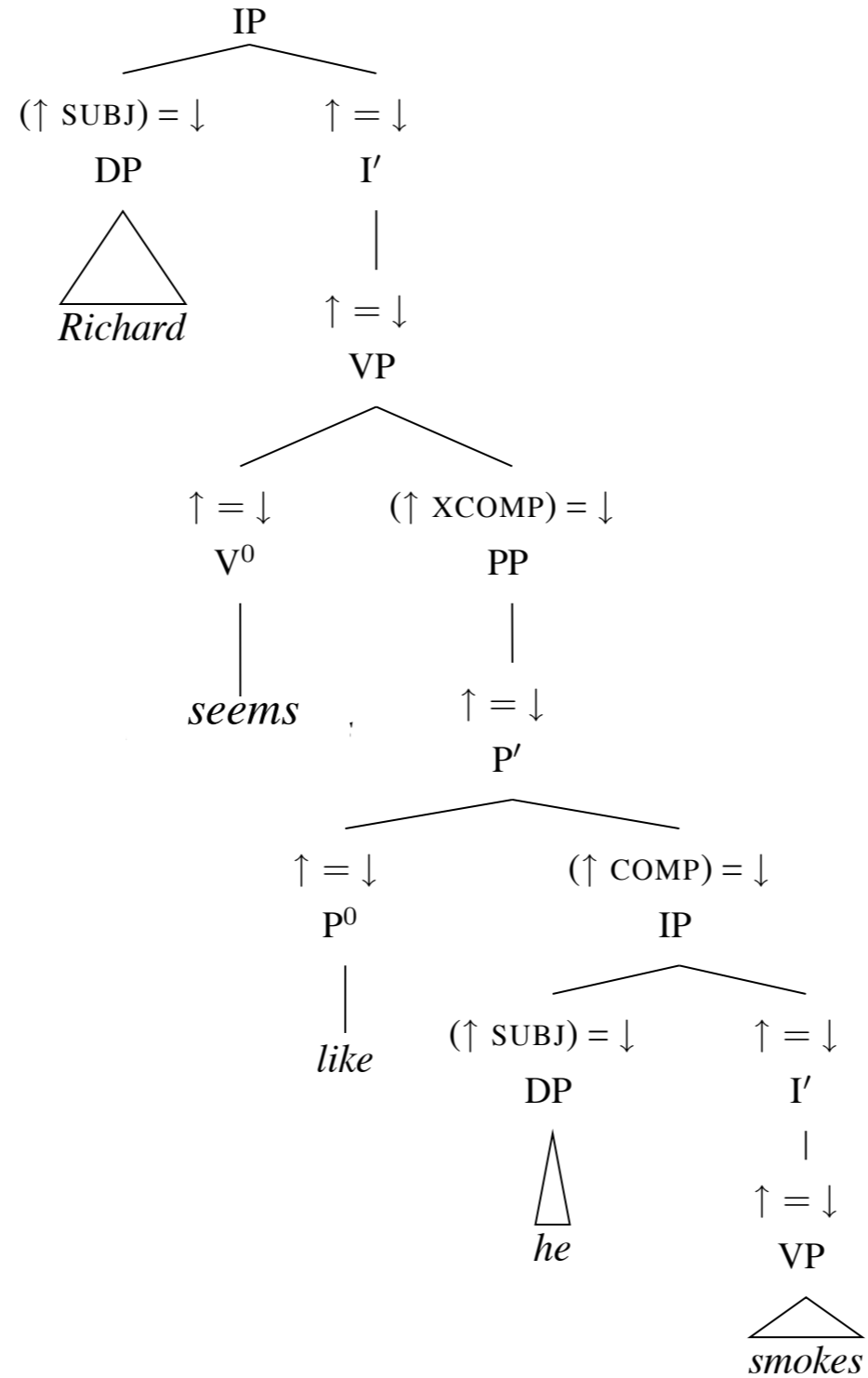
---

*like*<sub>1</sub>    P<sup>0</sup>    (↑ PRED) = ‘like⟨SUBJ,COMP⟩’

*like*<sub>2</sub>    P<sup>0</sup>    (↑ PRED) = ‘like⟨CF⟩SUBJ’  
{ (↑ SUBJ) = (↑ XCOMP SUBJ) |  
  (↑ SUBJ PRONTYPE) = EXPLETIVE  
  (↑ SUBJ FORM) = IT  
  (↑ COMP) }

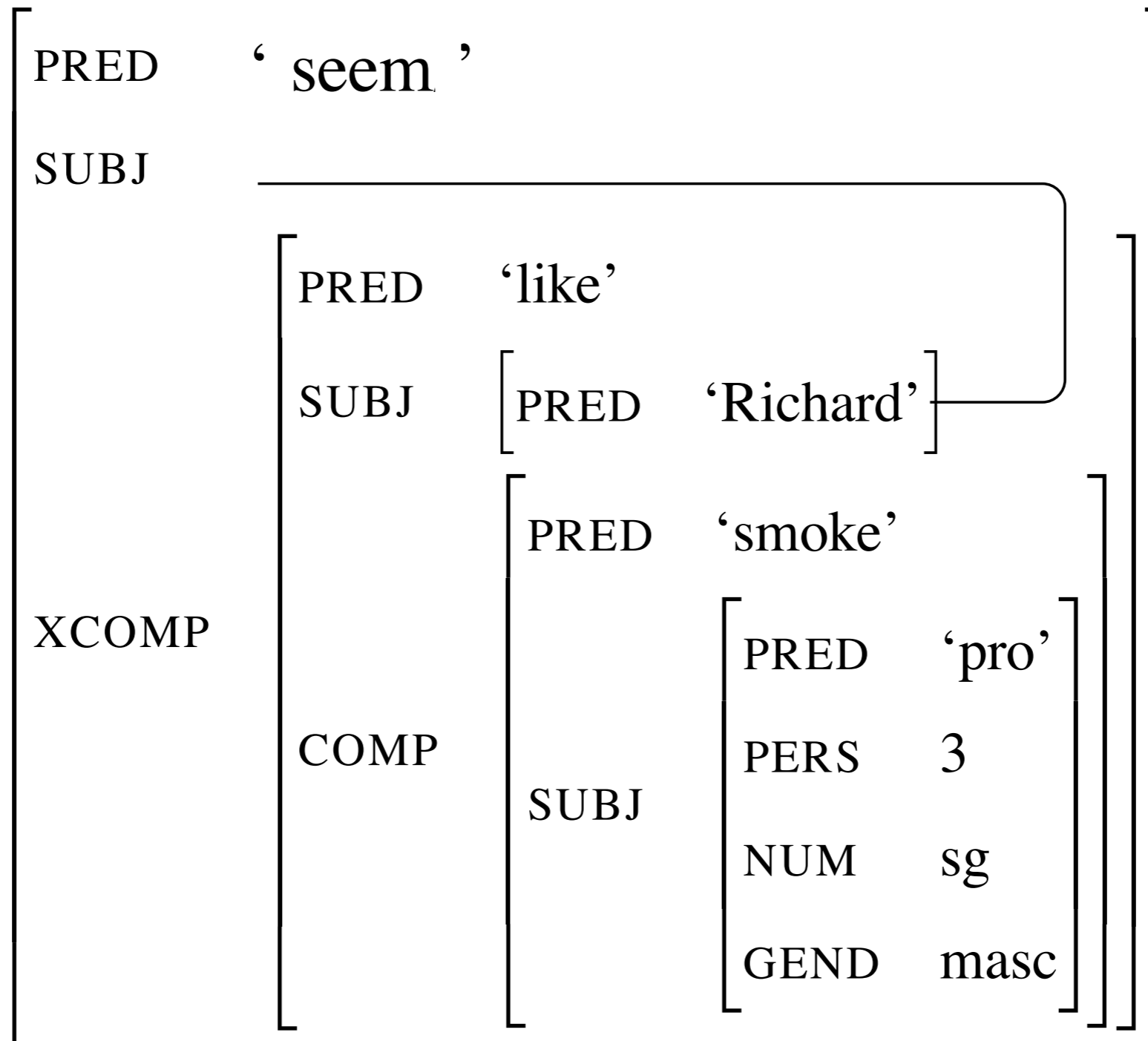
# C-structure

---



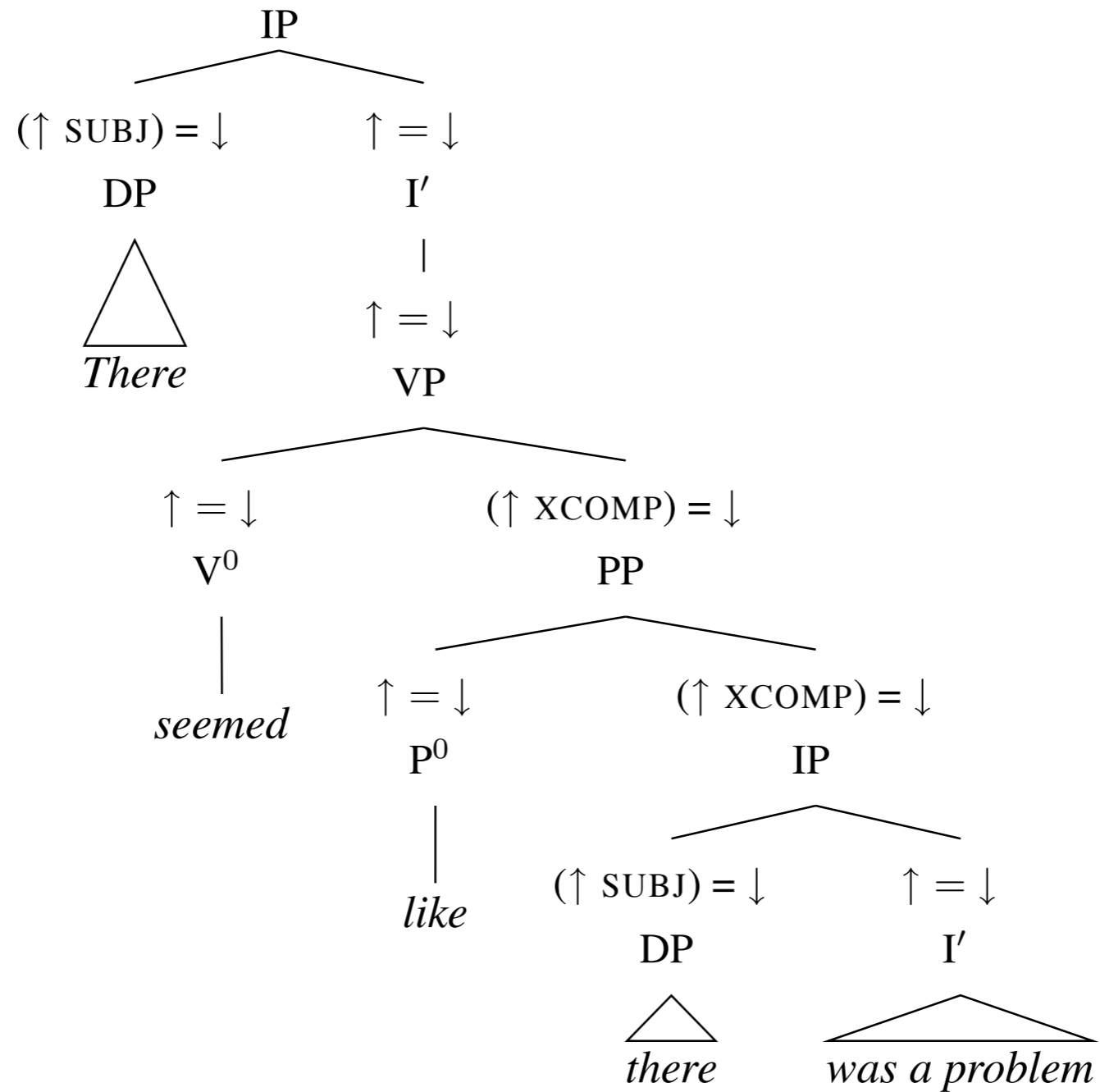
# F-structure

---



# C-structure

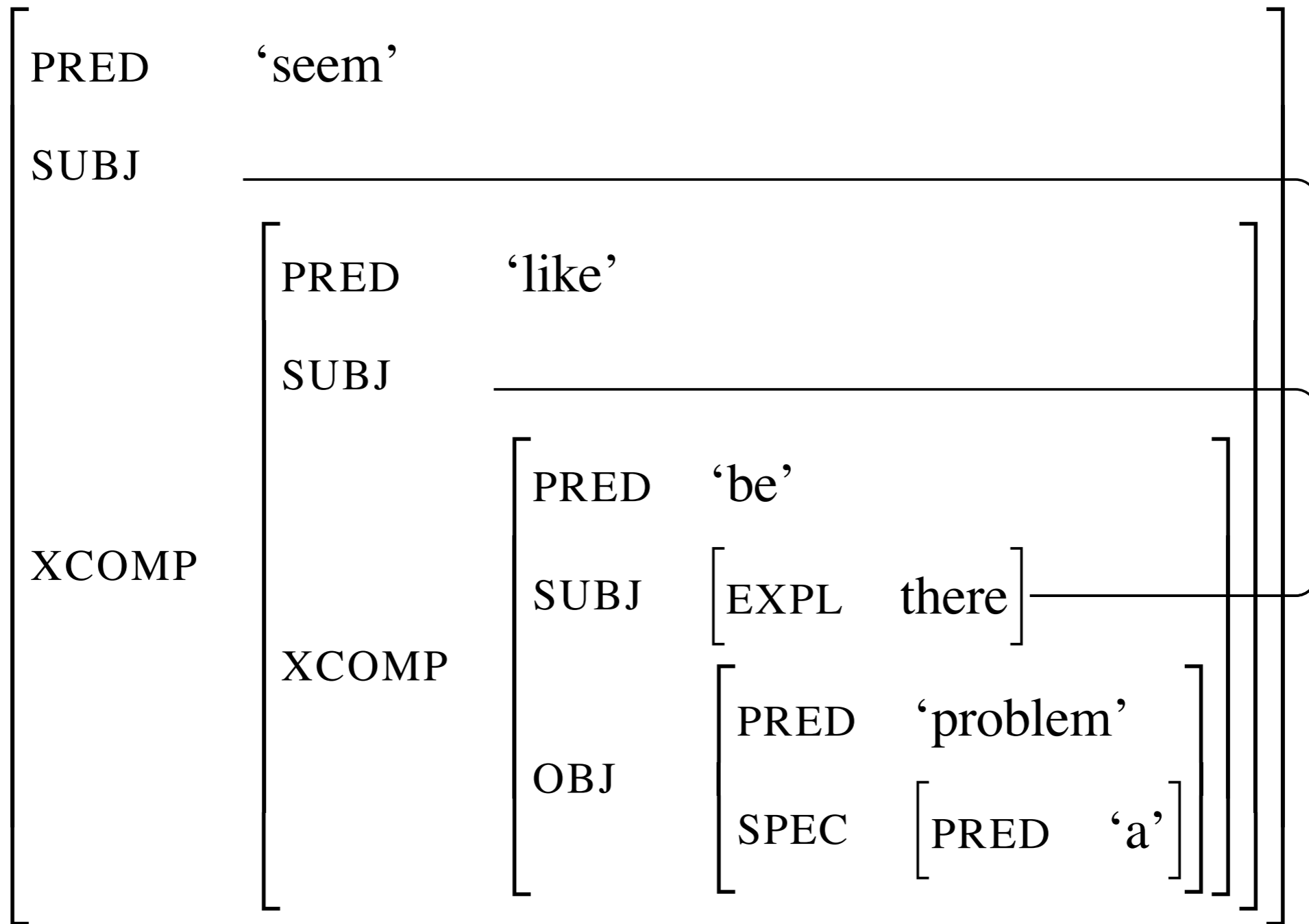
---





# F-structure

---



# Unbounded Dependencies

# Filler-Gap Dependencies

# Functional Uncertainty

---

- The syntactic relationship between the top and bottom of an unbounded dependency is represented with a functional uncertainty:
- Top = MiddlePath-Func-Uncertainty Bottom-Func-Uncertainty

(1) [What] [did Kim claim that Sandy suspected that Robin knew] []

top

middle

bottom

$$(\uparrow \text{FOCUS}) = (\uparrow \text{COMP}^* \{ \text{OBJ} | \text{OBJ}_\theta \})$$

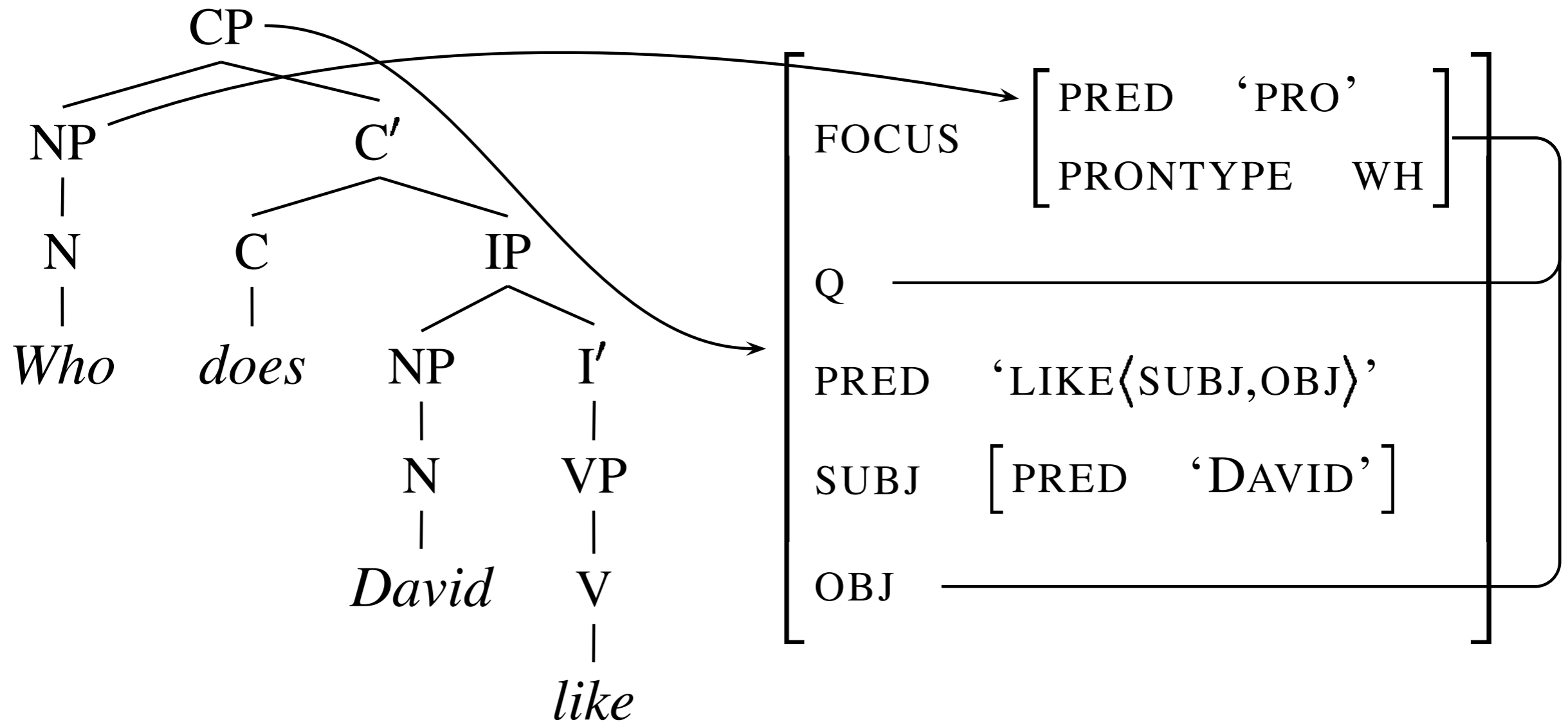
top

middle

bottom

(2) [What] [did Kim claim that Sandy suspected that Robin gave Bo] []

# Wh-Questions: Example



# Wh-Questions: Annotated PS Rule

---

$$\text{CP} \rightarrow \left( \begin{array}{c} \text{QuesP} \\ (\uparrow \text{ FOCUS}) = \downarrow \\ (\uparrow \text{ FOCUS}) = (\uparrow \text{ QFOCUSPATH}) \\ (\uparrow \text{ Q}) = (\uparrow \text{ FOCUS WHPATH}) \\ (\uparrow \text{ Q PRONTYPE}) =_c \text{ WH} \end{array} \right) \left( \begin{array}{c} \text{C}' \\ \uparrow = \downarrow \end{array} \right)$$

# *Wh*-Questions: QuesP Metacategory

---

**QuesP  $\equiv$  {NP | PP | AdvP | AP}**

(1) NP: Who do you like?

(2) PP: To whom did you give a book?

(3) AdvP: When did you yawn?

(4) AP: How tall is Chris?

# Wh-Questions: Unbounded Dependency Equation

---

English QFOCUSPATH:

$$\left\{ \text{XCOMP} \mid \begin{array}{c} \text{COMP} \\ (\rightarrow \text{LDD}) \neq - \end{array} \mid \begin{array}{c} \text{OBJ} \\ (\rightarrow \text{TENSE}) \end{array} \right\}^* \left\{ (\text{ADJ} \rightarrow \text{TENSE}) \in \text{GF} \mid \text{GF} \right\}$$



# Wh-Questions: Pied Piping

---

English WHPATH:

{SPEC\* | OBJ}

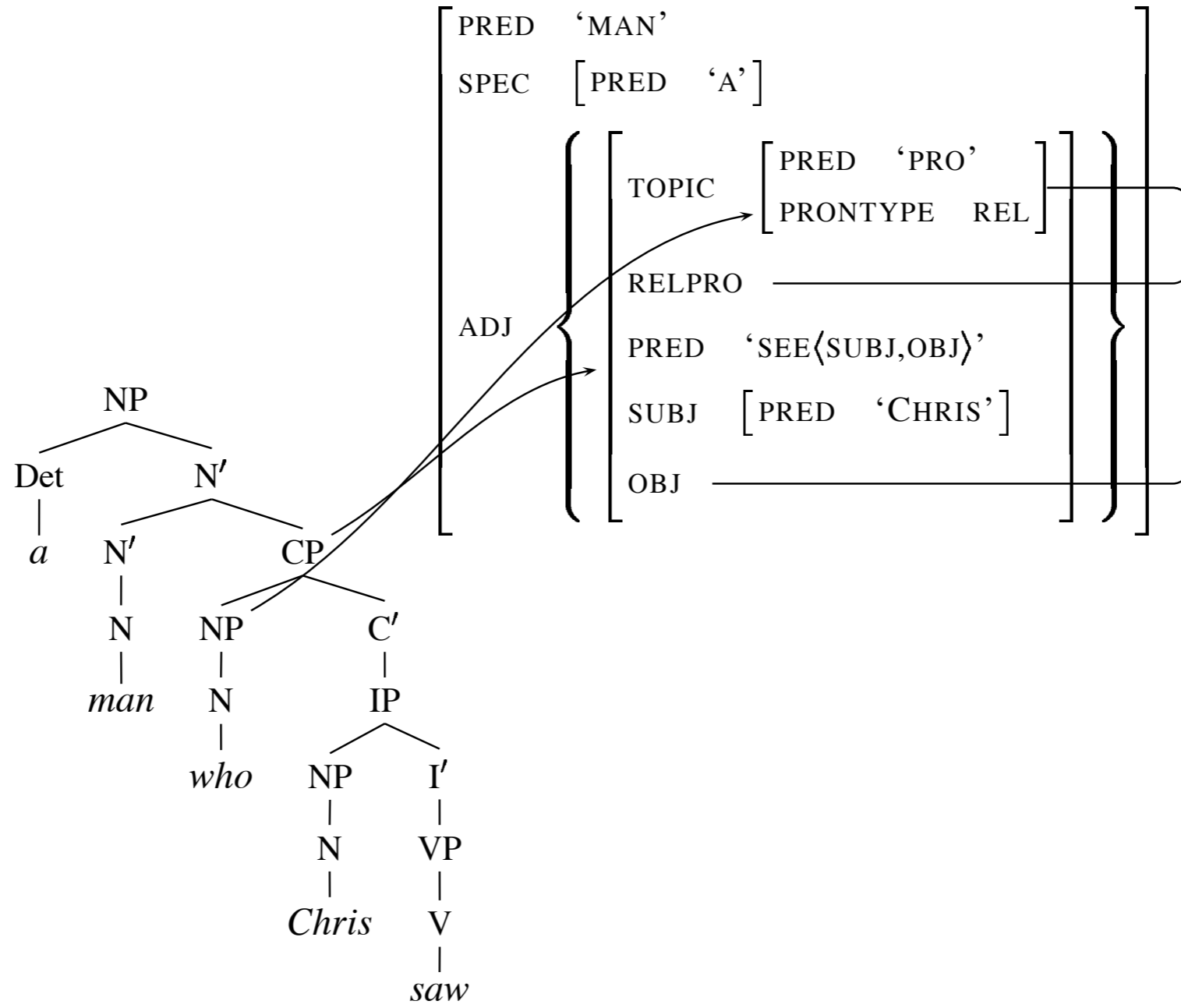
(1) [Whose book] did you read?

(2) [Whose brother's book] did you read?

(3) [In which room] do you teach?

# Relative Clauses: Example

*a man who Chris saw*



# Relative Clauses: Annotated PS Rule

---

$$\text{CP} \longrightarrow \left( \begin{array}{c} \text{RelP} \\ (\uparrow \text{ TOPIC}) = \downarrow \\ (\uparrow \text{ TOPIC}) = (\uparrow \text{ RTOPICPATH}) \\ (\uparrow \text{ RELPRO}) = (\uparrow \text{ TOPIC RELPATH}) \\ (\uparrow \text{ RELPRO PRONTYPE}) =_c \text{ REL} \end{array} \right) \left( \begin{array}{c} \text{C}' \\ \uparrow = \downarrow \end{array} \right)$$

# Relative Clauses: RelP Metacategory

---

$\text{RelP} \equiv \{\text{NP} \mid \text{PP} \mid \text{AP} \mid \text{AdvP}\}$

(1) NP: a man who I selected

(2) PP: a man to whom I gave a book

(3) AP: the kind of person proud of whom I could never be

(4) AdvP: the city where I live

# Relative Clauses: Unbounded Dependency Equation

---

English RTOPICPATH:

$$\left\{ \text{XCOMP} \mid \begin{array}{c} \text{COMP} \\ (\rightarrow \text{LDD}) \neq - \end{array} \mid \begin{array}{c} \text{OBJ} \\ (\rightarrow \text{TENSE}) \end{array} \right\}^* \left\{ \begin{array}{c} (\text{ADJ} \in \quad) \\ \neg(\rightarrow \text{TENSE}) \end{array} \mid (\text{GF}) \mid \text{GF} \right\}$$

# Relative Clauses: Pied Piping

---

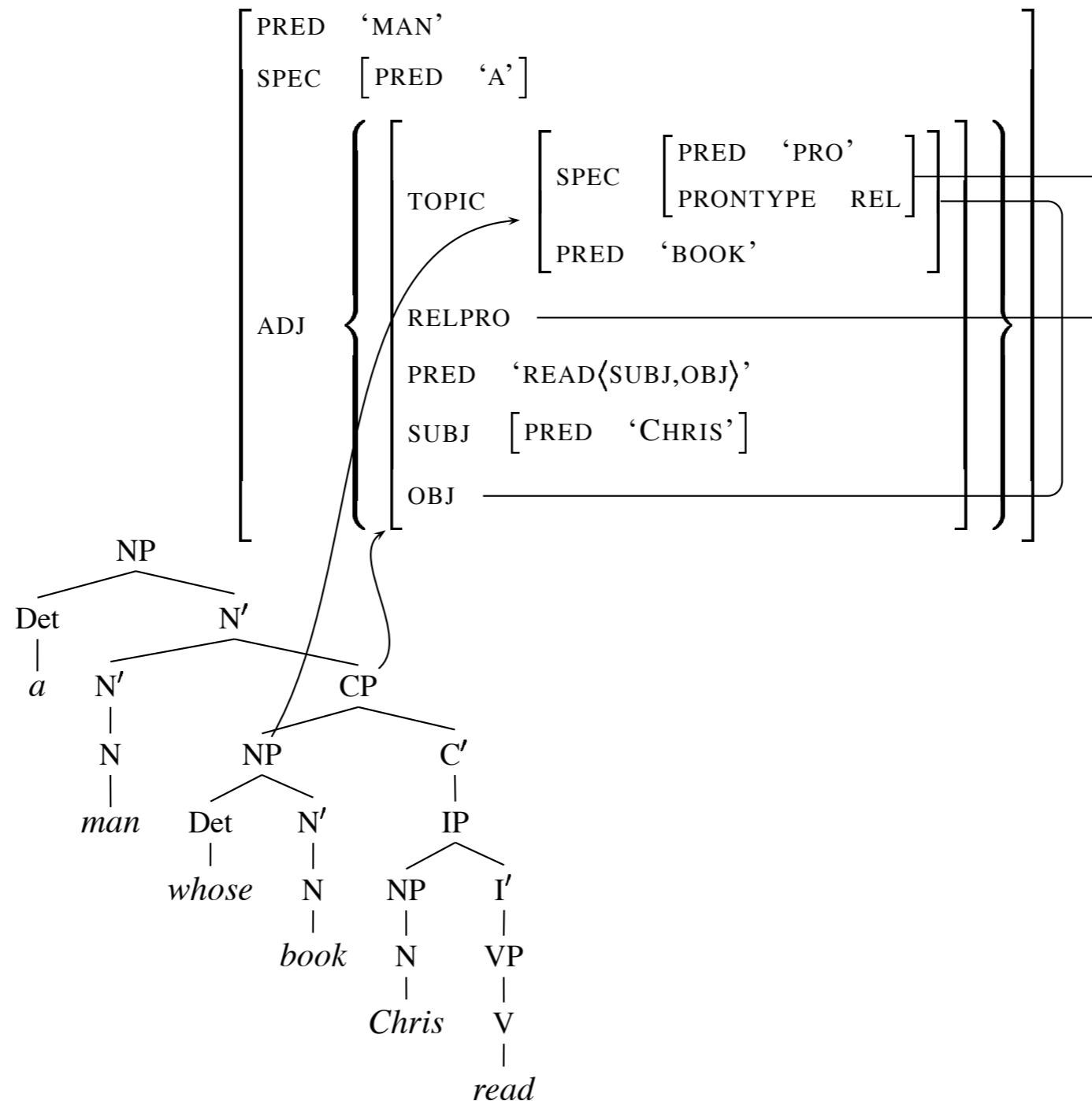
English RELPATH:

$\{ \text{SPEC}^* \mid [(\text{OBL}_\theta)\text{OBJ}]^* \}$

- (1) the man [who] I met
- (2) the man [whose book] I read
- (3) the man [whose brother's book] I read
- (4) the report [the cover of which] I designed
- (5) the man [faster than whom] I can run
- (6) the kind of person [proud of whom] I could never be
- (7) the report [the height of the lettering on the cover of which] the government prescribes

# Relative Clauses: Pied Piping Example

*a man whose book Chris read*



# Constraints on Extraction



# Empty Category Principle/*That*-Trace

---

(1) Who do you think [\_\_ left]?

(2)\* Who do you think [that \_\_ left]?

(3)\* What do you wonder [if \_\_ smells bad]?

(4) Who do you think [\_\_ should be trusted]?

(5)\* Who do you think [that \_\_ should be trusted]?

(6) Who do you think [that, under no circumstances, \_\_ should be trusted]?

(7) Who do you wonder [if, under certain circumstances, \_\_ could be trusted]?

# That-Trace in LFG

---

- LFG has a relation called f-precedence that uses the native precedence of c-structure to talk about precedence between bits of f-structure.
- F-precedence relies on LFG's projection architecture and the inverse of the c-structure–f-structure mapping function  $\phi$ .
- The inverse is written  $\phi^{-1}$  and returns the set of c-structure nodes that map to its argument f-structure node.

## **F-precedence**

An f-structure  $f$  f-precedes an f-structure  $g$  ( $f <_f g$ ) if and only if for all  $n_1 \in \phi^{-1}(f)$  and for all  $n_2 \in \phi^{-1}(g)$ ,  $n_1$  c-precedes  $n_2$ .



# *That-Trace* in LFG

---

- Assume a native precedence relation on strings, yielding a notion of element that is string-adjacent to the right ('next string element'), which we define as  $\text{Right}_{\text{string}}(\pi^{-1}(*))$ , where  $*$  designates the current c-structure node in a phrase structure rule element or lexical entry.
- Let's abbreviate the right string-adjacent element to  $*$  as  $>$ .
- The semantics of  $>$  is 'the string element that is right string-adjacent to me'.
- Note that  $\pi^{-1}$  returns string elements, not sets of string elements, because  $\pi$  is bijective, since c-structures are trees.

# *That-Trace* in LFG

---

- We can use f-precedence and  $>$  to capture the surfacy nature of *That-Trace*.
- Basically, English has a (somewhat arbitrary) constraint that the right-adjacent string element to the complementizer must be locally realized.
- This can be stated by requiring that any unbounded dependency function in the f-structure corresponding to the element that occurs in the string immediately after the complementizer should **not** f-precede the complementizer's f-structure.

# Left Branch Constraint

---

(1) Whose car did you drive \_\_\_?

(2)\* Whose did you drive [\_\_\_ car]?

# Left Branch Constraint in LFG

---

- Do not include SPEC/POSS in GFs of possible extraction sites.
- Note that the equation we looked at previously already disallows the extraction from passing through a SPEC in the first part.
- We modify the equation as follows

$$\left\{ \text{XCOMP} \mid \begin{array}{c} \text{COMP} \\ (\rightarrow \text{LDD}) \neq - \end{array} \mid \begin{array}{c} \text{OBJ} \\ (\rightarrow \text{TENSE}) \end{array} \right\}^* \left\{ \left( \begin{array}{c} \text{ADJ} \\ \neg(\rightarrow \text{TENSE}) \end{array} \in \right) \mid \text{GF} \mid \text{GF} - \text{SPEC} \right\}$$

# Wh-Islands in LFG: Off-Path Constraints

---

- The off-path metavariable  $\leftarrow$  refers to the f-structure that contains the attribute that the constraint is attached to.
- The off-path metavariable  $\rightarrow$  refers to the f-structure that is the value of the attribute that the constraint is attached to.

$$\left\{ \text{XCOMP} \mid \begin{array}{c} \text{COMP} \\ (\rightarrow \text{LDD}) \neq - \end{array} \mid \begin{array}{c} \text{OBJ} \\ (\rightarrow \text{TENSE}) \end{array} \right\}^* \left\{ (\text{ADJ} \in \quad) \quad (\text{GF}) \mid \text{GF} - \text{SPEC} \right\} \\ \neg(\rightarrow \text{TENSE})$$

- Use  $\leftarrow$  to state the bottom cannot be in an f-structure that has an unbounded dependency function UDF, where  $\text{UDF} = \{\text{TOPIC} \mid \text{FOCUS}\}$ .

$$\left\{ \text{XCOMP} \mid \begin{array}{c} \text{COMP} \\ (\rightarrow \text{LDD}) \neq - \end{array} \mid \begin{array}{c} \text{OBJ} \\ (\rightarrow \text{TENSE}) \end{array} \right\}^* \left\{ (\text{ADJ} \in \quad) \quad (\text{GF}) \mid \text{GF} - \text{SPEC} \right\} \\ \neg(\rightarrow \text{TENSE}) \quad \neg(\leftarrow \text{UDF})$$



# Successive Cyclic Effects

# Successive Cyclicity

---

- Data from languages such as Irish and Chamorro, which show successive marking along the extraction path, have motivated the claim that extraction/movement is ‘cyclic’ (not all at once). Cf. Phases in Minimalism.
- Of course, this data does not argue for movement per se, as some have wrongly assumed, but rather that unbounded dependencies should
  1. Be made up of a series of local relations; or
  2. Have a way to refer to their environments as the dependency is constructed.
- HPSG has adopted the first approach, LFG the second.

# Data: Irish

---

- Note: Date from McCloskey via Bouma et al. (2001).

a. Shíl mé *goN* mbeadh sé ann  
*thought I PRT would-be he there*

I thought that he would be there.

b. Dúirt mé *gurL* shíl mé *goN* mbeadh sé ann  
*said I goN+PAST thought I PRT would-be he there*

I said that I thought that he would be there.

c. an fear *aL* shíl mé *aL* bheadh \_\_ ann  
*[the man]<sub>j</sub> PRT thought I PRT would-be \_\_<sub>j</sub> there*

the man that I thought would be there

d. an fear *aL* dúirt mé *aL* shíl mé *aL* bheadh \_\_ ann  
*[the man]<sub>j</sub> PRT said I PRT thought I PRT would-be \_\_<sub>j</sub> there*

The man that I said I thought would be there

e. an fear *aL* shíl \_\_ *goN* mbeadh sé ann  
*[the man]<sub>j</sub> PRT thought \_\_<sub>j</sub> PRT would-be he there*

the man that thought he would be there

# Irish Successive Cyclicity in LFG

---

$$aL \quad \hat{C} \quad (\uparrow \text{UDF}) = (\uparrow \text{CF}^* \text{GF})$$
$$(\rightarrow \text{UDF}) = (\uparrow \text{UDF})$$

Note: UDF = {TOPIC | FOCUS}, CF = {XCOMP | COMP}

$$goN \quad \hat{C} \quad (\uparrow \text{TENSE})$$
$$\neg(\uparrow \text{UDF})$$

# Glue Semantics

# Glue Semantics

---

- Glue Semantics is a type-logical semantics that can be tied to any syntactic formalism that supports a notion of headedness.
- Glue Semantics can be thought of as *categorial semantics without categorial syntax*.
- The independent syntax assumed in Glue Semantics means that the logic of composition is *commutative*, unlike in Categorical Grammar.
- Selected works:  
Dalrymple (1999, 2001), Crouch & van Genabith (2000),  
Asudeh (2004, 2005a,b, in prep.), Lev 2007, Kokkonidis (in press)

# Glue Semantics

---

- Lexically-contributed *meaning constructors* :=

Meaning language term       $\mathcal{M} : G$       Composition language term

- Meaning language := some lambda calculus
  - Model-theoretic
- Composition language := linear logic
  - Proof-theoretic
- Curry Howard Isomorphism between formulas (meanings) and types (proof terms)
- Successful Glue Semantics proof:

$$\Gamma \vdash \mathcal{M} : G_t$$

# Key Glue Proof Rules with Curry-Howard Terms

---

Application : Implication Elimination

$$\frac{\begin{array}{c} \vdots \\ a : A \end{array} \quad \begin{array}{c} \vdots \\ f : A \multimap B \end{array}}{f(a) : B} \multimap_{\mathcal{E}}$$

Abstraction : Implication Introduction

$$\frac{\begin{array}{c} [x : A]^1 \\ \vdots \\ f : B \end{array}}{\lambda x. f : A \multimap B} \multimap_{\mathcal{I},1}$$

Pairwise Substitution : Conjunction Elimination

$$\frac{\begin{array}{c} \vdots \\ a : A \otimes B \end{array} \quad \begin{array}{c} [x : A]^1 \quad [y : B]^2 \\ \vdots \\ f : C \end{array}}{\text{let } a \text{ be } x \times y \text{ in } f : C} \otimes_{\mathcal{E},1,2}$$

Beta reduction for let:

$$\text{let } a \times b \text{ be } x \times y \text{ in } f \Rightarrow_{\beta} f[a/x, b/y]$$



# Example: *Mary laughed*

1.  $mary : \uparrow_{\sigma_e}$

2.  $laugh : (\uparrow \text{SUBJ})_{\sigma_e} \multimap \uparrow_{\sigma_t}$

1'.  $mary : g_{\sigma_e}$

2'.  $laugh : g_{\sigma_e} \multimap f_{\sigma_t}$

$$f \left[ \begin{array}{ll} \text{PRED} & \text{'laugh' \langle \text{SUBJ} \rangle} \\ \text{SUBJ} & g \left[ \text{PRED} \quad \text{'Mary'} \right] \end{array} \right]$$

1''.  $mary : m$

2''.  $laugh : m \multimap l$

Proof

1.  $mary : m$

Lex. **Mary**

2.  $laugh : m \multimap l$

Lex. **laughed**

3.  $laugh(mary) : l$

E  $\multimap$ , 1, 2

$\equiv$

Proof

$mary : m$

$laugh : m \multimap l$

---

$\multimap_{\varepsilon}$

$laugh(mary) : l$

# Example: *Most presidents speak*

---

1.  $\lambda R \lambda S. most(R, S) : (v \multimap r) \multimap \forall X. [(p \multimap X) \multimap X]$       **Lex. most**
2.  $president^* : v \multimap r$       **Lex. presidents**
3.  $speak : p \multimap s$       **Lex. speak**

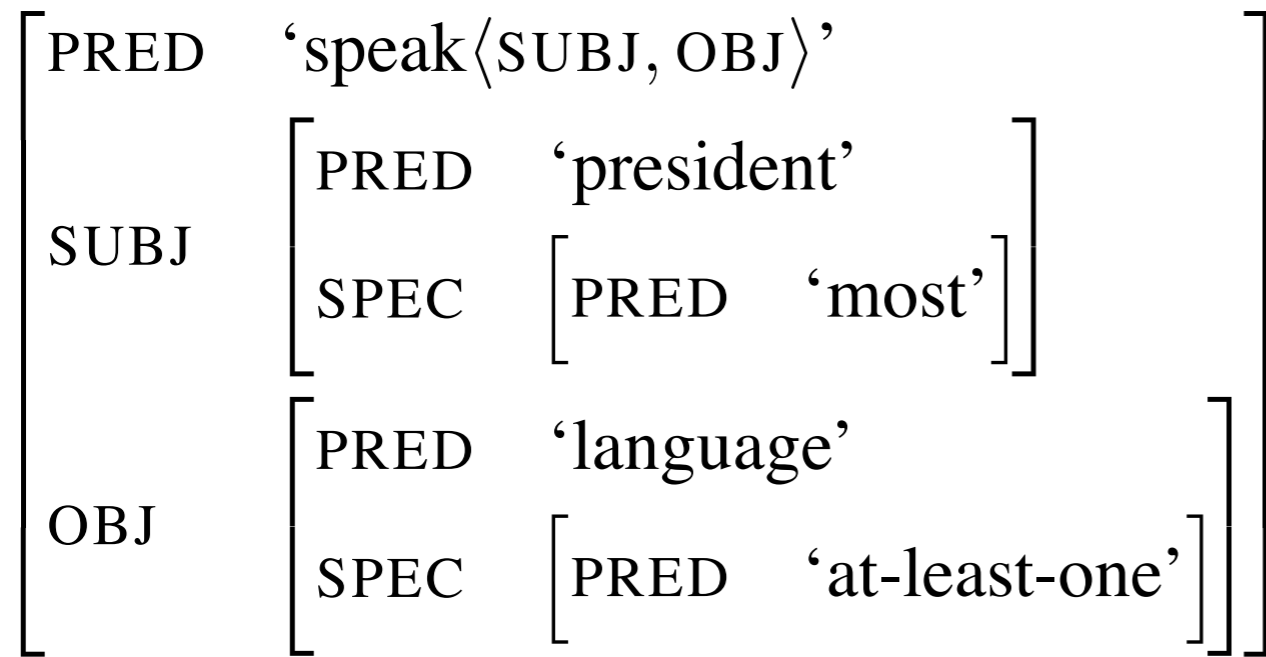
$$\frac{\lambda R \lambda S. most(R, S) : (v \multimap r) \multimap \forall X. [(p \multimap X) \multimap X] \quad president^* : v \multimap r}{}$$

$$\frac{\lambda S. most(president^*, S) : \forall X. [(p \multimap X) \multimap X] \quad speak : p \multimap s}{most(president^*, speak) : s} \multimap \varepsilon, [s/X]$$

# Example:

*Most presidents speak at least one language*

---



Single parse



Multiple scope possibilities  
(Underspecification through  
quantification)

1.  $\lambda R \lambda S. \text{most}(R, S) :$   
 $(v1 \multimap r1) \multimap \forall X. [(p \multimap X) \multimap X]$
2.  $\text{president}^* : v1 \multimap r1$
3.  $\text{speak} : p \multimap l \multimap s$
4.  $\lambda P \lambda Q. \text{at-least-one}(P, Q) :$   
 $(v2 \multimap r2) \multimap \forall Y. [(l \multimap Y) \multimap Y]$
5.  $\text{language} : v2 \multimap r2$

Lex. **most**

Lex. **presidents**

Lex. **speak**

Lex. **at least one**

Lex. **language**

# Most presidents speak at least one language

## Subject wide scope

$$\begin{array}{c}
 \lambda R \lambda S. \text{most}(R, S) : \\
 (v1 \multimap r1) \multimap \forall X. [(p \multimap X) \multimap X] \\
 \hline
 \lambda S. \text{most}(\text{president}^*, S) : \\
 \forall X. [(p \multimap X) \multimap X] \\
 \hline
 \text{most}(\text{president}^*, \lambda z. a-l-o(\text{lang}, \lambda y. \text{speak}(z, y))) : s
 \end{array}
 \quad
 \begin{array}{c}
 \lambda P \lambda Q. a-l-o(P, Q) : \\
 (v2 \multimap r2) \multimap \forall Y. [(l \multimap Y) \multimap Y] \\
 \hline
 \lambda Q. a-l-o(\text{lang}, Q) : \\
 \forall Y. [(l \multimap Y) \multimap Y] \\
 \hline
 a-l-o(\text{lang}, \lambda y. \text{speak}(z, y)) : s \\
 \hline
 \lambda z. a-l-o(\text{lang}, \lambda y. \text{speak}(z, y)) : p \multimap s \\
 \hline
 [s/X]
 \end{array}
 \quad
 \begin{array}{c}
 \text{lang} : \\
 v2 \multimap r2 \\
 \hline
 \lambda x \lambda y. \text{speak}(x, y) : \\
 p \multimap l \multimap s \\
 [z : p]^1 \\
 \hline
 \lambda y. \text{speak}(z, y) : \\
 l \multimap s \\
 \hline
 [s/Y]
 \end{array}
 \quad
 \begin{array}{c}
 \lambda x \lambda y. \text{speak}(x, y) : \\
 p \multimap l \multimap s \\
 [z : p]^1 \\
 \hline
 \lambda y. \text{speak}(z, y) : \\
 l \multimap s \\
 \hline
 [s/Y]
 \end{array}$$

# Most presidents speak at least one language

## Object wide scope

$$\begin{array}{c}
 \lambda P \lambda Q. a-l-o(P, Q) : \\
 (v2 \multimap r2) \multimap \forall Y. [(l \multimap Y) \multimap Y] \\
 \hline
 \lambda Q. a-l-o(lang, Q) : \\
 \forall Y. [(l \multimap Y) \multimap Y] \\
 \hline
 a-l-o(lang, \lambda z. most(president^*, \lambda x. speak(x, z))) : s
 \end{array}
 \quad
 \begin{array}{c}
 \lambda R \lambda S. most(R, S) : \\
 (v1 \multimap r1) \multimap \forall X. [(p \multimap X) \multimap X] \\
 \hline
 \lambda S. most(president^*, S) : \\
 \forall X. [(p \multimap X) \multimap X] \\
 \hline
 most(president^*, \lambda x. speak(x, z)) : s \\
 \hline
 \lambda z. most(president^*, \lambda x. speak(x, z)) : l \multimap s \\
 \hline
 a-l-o(lang, \lambda z. most(president^*, \lambda x. speak(x, z))) : s
 \end{array}
 \quad
 \begin{array}{c}
 president^* : \\
 v1 \multimap r1 \\
 \hline
 \lambda y \lambda x. speak(x, y) : \\
 l \multimap p \multimap s \\
 \hline
 \lambda x. speak(x, z) : \\
 p \multimap s \\
 \hline
 \lambda z. most(president^*, \lambda x. speak(x, z)) : l \multimap s \\
 \hline
 \lambda z. most(president^*, \lambda x. speak(x, z)) : l \multimap s \\
 \hline
 \lambda z. most(president^*, \lambda x. speak(x, z)) : l \multimap s
 \end{array}
 \quad
 \begin{array}{c}
 [z : l]^1 \\
 [s/X] \\
 \multimap_{\mathcal{I},1} \\
 [s/Y]
 \end{array}$$

# Anaphora in Glue Semantics

---

- Variable-free: pronouns are functions on their antecedents (Jacobson 1999, among others)
- Commutative logic of composition allows pronouns to compose **directly** with their antecedents.
- No need for otherwise unmotivated additional type shifting (e.g. Jacobson's z-shift)

# Anaphora in Glue Semantics

---

1. Joe said he bowls.

- Pronominal meaning constructor:

$$\lambda z.z \times z : A \multimap (A \otimes P)$$

$$\begin{array}{c}
 \begin{array}{c}
 \textit{joe} : \quad \lambda z.z \times z : \\
 \textit{j} \quad \quad \textit{j} \multimap (\textit{j} \otimes \textit{p})
 \end{array} \\
 \hline
 \textit{joe} \times \textit{joe} : \textit{j} \otimes \textit{p}
 \end{array}
 \quad
 \begin{array}{c}
 \begin{array}{c}
 [x : \textit{j}]^1 \quad \lambda u \lambda q. \textit{say}(u, q) : \\
 \textit{j} \multimap \textit{b} \multimap \textit{s}
 \end{array} \\
 \hline
 \begin{array}{c}
 \lambda q. \textit{say}(x, q) : \\
 \textit{b} \multimap \textit{s}
 \end{array}
 \end{array}
 \quad
 \begin{array}{c}
 \begin{array}{c}
 [y : \textit{p}]^2 \quad \lambda v. \textit{bowl}(v) : \\
 \textit{p} \multimap \textit{b}
 \end{array} \\
 \hline
 \begin{array}{c}
 \textit{bowl}(y) : \\
 \textit{b}
 \end{array}
 \end{array} \\
 \hline
 \begin{array}{c}
 \textit{joe} \times \textit{joe} : \textit{j} \otimes \textit{p} \quad \textit{say}(x, \textit{bowl}(y)) : \textit{s} \\
 \hline
 \textit{let } \textit{joe} \times \textit{joe} \textit{ be } x \times y \textit{ in } \textit{say}(x, \textit{bowl}(y)) : \textit{s} \\
 \hline
 \textit{say}(\textit{joe}, \textit{bowl}(\textit{joe})) : \textit{s} \quad \Rightarrow \beta
 \end{array}
 \quad \otimes \varepsilon_{1,2}
 \end{array}$$

# Further Points of Interest

---

- Glue Semantics can be understood as a *representationalist* theory, picking up on a theme from Wednesday's semantics workshop.
  - Proofs can be reasoned about as representations (Asudeh & Crouch 2002a,b).
  - Proofs have strong identity criteria: normalization, comparison
- Glue Semantics allows recovery of a non-representationalist notion of *direct compositionality* (Asudeh 2005, 2006).
  - ➔ Flexible framework with lots of scope for exploration of questions of compositionality and semantic representation