## Lexical-Functional Grammar

## \&

## Flexible Composition

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## Goals

- Provide an overview of Lexical-Functional Grammar
- Provide an overview of Glue Semantics
- Provide an introduction to an approach to argument structure that builds on these two theories, part of what I call Flexible Composition


## Lexical-Functional Grammar

## History

- LFG was developed by Joan Bresnan, a syntactician, and Ron Kaplan, a social psychologist by training but then a computational linguist, as a constraint-based/declarative alternative to transformational/procedural theories of the time.
- Desiderata:
- Formal precision
- Psychological plausibility
- Computational tractability


## Overview

- At the heart of LFG remain its two syntactic structures:
- C (onstituent)-structure
- 'Concrete syntax’: Precedence, dominance, constituency
- F (unctional)-structure
- 'Abstract syntax’: Morphosyntactic features, grammatical functions, predication, subcategorization, local dependencies (agreement, control, raising), unbounded dependencies, anaphoric syntax (binding)


## The $\phi$ correspondence function

- Elements of the c-structure are mapped to (put into correspondence with) elements of the f-structure by the $\phi$ correspondence function (sometimes called a projection function).
- This is accomplished by adding functional descriptions to the nodes in the c-structure tree.
- These equations use the $\uparrow$ ("up arrow") and $\downarrow$ ("down arrow") metavariables.
- A $\uparrow$ on a c-structure node $n$ refers to the $f$-structure of the (c-structure) mother of $n$.
- $\quad A \downarrow$ on a c-structure node $n$ refers to the $f$-structure of node $n$.
- Examples:
- $\quad \uparrow=\downarrow$ on $n$ means that $n$ and $n$ 's mother map to the same $f$-structure.
- $\quad(\uparrow$ SUBJECT $)=\downarrow$ on $n$ means that the $f$-structure of $n$ is the value of the SUBJECT attribute in the $f$-structure of $n$ 's mother.


## Example:

## That kid is eating cake



## Lexical entries

that, $\mathrm{D}^{0}$
$(\uparrow$ DEFINITE $)=+$
$(\uparrow$ DEIXIS $)=$ DISTAL
$(\uparrow$ NUMBER $)=$ SG
$(\uparrow$ PERSON $)=3$
$\begin{aligned} \text { kid }, \mathrm{N}^{0} \quad & (\uparrow \text { PRED })=\text { 'kid } \\ & (\uparrow \text { NUMBER })=\mathrm{SG} \\ & (\uparrow \text { PERSON })=3\end{aligned}$
$i s, \mathrm{I}^{0} \quad(\uparrow$ SUBJ NUMBER $)=\mathrm{SG}$
$(\uparrow$ SUBJ PERSON $)=3$
$(\uparrow$ TENSE $)=$ PRESENT
$(\uparrow$ PARTICIPLE $)={ }_{c}$ PRESENT
eating, $\mathrm{V}^{0} \quad(\uparrow$ PRED $)=$ 'eat $\langle$ SUBJ, OBJ $\rangle$ '
$(\uparrow$ ASPECT $)=$ PROGRESSIVE
$(\uparrow$ PARTICIPLE $)=$ PRESENT
cake, $\mathrm{N}^{0} \quad(\uparrow$ PRED $)=$ 'cake ${ }^{\prime}$
$(\uparrow$ NUMBER $)=\mathrm{SG}$
$(\uparrow$ PERSON $)=3$

## Example:

## That kid is eating cake



## Flexibility in mapping



## Example: the book that she likes

C-structure rules

| DP $\longrightarrow$ | $\begin{gathered} \mathrm{D}^{0} \\ \uparrow=\downarrow \end{gathered}$ | $\begin{gathered} \mathrm{NP} \\ \uparrow=\downarrow \end{gathered}$ |
| :---: | :---: | :---: |
| NP $\longrightarrow$ | $\begin{gathered} \mathrm{NP} \\ \uparrow=\downarrow \end{gathered}$ | $\begin{gathered} \mathrm{CP} \\ \downarrow \in(\uparrow \mathrm{ADJ}) \end{gathered}$ |
| NP $\longrightarrow$ | $\begin{gathered} \mathrm{N}^{\prime} \\ \uparrow=\downarrow \end{gathered}$ |  |
| $\mathrm{N}^{\prime} \longrightarrow$ | $\begin{gathered} \mathrm{N}^{0} \\ \uparrow=\downarrow \end{gathered}$ |  |

C-structure and corresponding f-structure


# Example: the book that she likes 

## Lexical entries

| she, $\mathrm{D}^{0} \quad$ | $(\uparrow$ PRED $)=$ 'pro' |
| ---: | :--- |
|  | $(\uparrow$ PERSON $)=3$ |
|  | $(\uparrow$ NUMBER $)=$ SINGULAR |
|  | $(\uparrow$ GENDER $)=$ FEMININE |
| likes, $\quad \mathrm{V}^{0} \quad$ | $(\uparrow$ PRED $)=$ 'like $\langle$ SUBJ,OBJ $\rangle '$ |
|  | $(\uparrow$ TENSE $)=$ PRESENT |
|  | $(\uparrow$ SUBJECT PERSON $)=3$ |
|  | $(\uparrow$ SUBJECT NUMBER $)=$ SINGULAR |

the, $\mathrm{D}^{0} \quad$| $(\uparrow$ Spec Pred $)=$ |
| :--- |
|  |
|  |
| $(\uparrow$ definite $)=+$ |

book, $\mathrm{N}^{0} \quad(\uparrow$ PRED $)={ }^{\text {'book }}$
$(\uparrow$ nUMber $)=$ singular

C-structure with lexical information and instantiated f-structure


## Example: the book that she likes

## Penultimate f-structure



Notes:
I.I often adopt the practice of labelling f -structures mnemonically with the first letter of the PRED value.
2. I often leave the subcategorization out of the PRED. (There's a principled reason for this; we can discuss it in question time.)

## General wellformedness constraints on f-structures

- Completeness

All subcategorized grammatical functions in a PRED feature must be present in the f-structure.

- Coherence

All grammatical functions that are present in the fstructure must be subcategorized by a PRED feature.

- Consistency (a.k.a. Uniqueness)

Each f-structure attribute has one value.

# Example: Violations of Completeness, Coherence, Consistency 



## Example: the book that she likes

Penultimate f-structure


## Unbounded dependencies

- Extended Coherence Condition An UNBOUNDED DEPENDENCY FUNCTION (UDF) must be linked to the semantic predicate argument structure of the sentence in which it occurs, either by functionally or by anaphorically binding an argument.



## Example: the book that she likes

Final f-structure


## Language as a form-meaning mapping: The Correspondence Architecture



## Templates: <br> Generalizations over named descriptions

- An LFG template is nothing more than a named functional description (i.e., a set of equations that describe linguistic structures).
- For any LFG grammar defined in terms of templates, we could construct a completely equivalent grammar which does not use templates, simply by replacing each template with the description that it abbreviates.
- The same grammatical descriptions would be associated with words and phrases in each of the two grammars, and the grammars would produce the same c -structures and f-structures for the words and phrases of the language.
- However, the grammar without templates would lack the means of expressing generalizations across lexical entries and grammar rules which templates make available.
- In sum:
- Templates name LFG grammatical descriptions such that the same description can be used in different parts of the grammar.
- The semantics of template calling/invocation is just substitution:The grammatical description that the template names is substituted where the template is called.


## Example: Present tense intransitive verbs

$$
\begin{aligned}
3 \mathrm{SG}= & (\uparrow \text { SUBJ NUM })=3 \\
& (\uparrow \text { SUBJ PERS })=\text { SG }
\end{aligned}
$$

| laughs | V | $\begin{aligned} & (\uparrow \text { PRED })=\text { 'laugh }\langle\text { SUBJ }\rangle ' \\ & (\uparrow \text { TENSE })=\text { PRESENT } \\ & @ 3 \text { SG } \end{aligned}$ |
| :---: | :---: | :---: |
| laugh | V | $\begin{aligned} & (\uparrow \text { PRED })=\text { 'laugh }\langle\text { SUBJ }\rangle ’ \\ & \{(\uparrow \text { TENSE })=\text { PRESENT } \\ & \quad \neg @ 3 \text { SG } \mid \\ & \neg(\uparrow \text { TENSE })\} \end{aligned}$ |

```
INTRANSITIVE (X) = (\uparrow PRED ) = 'X X SUBJ }\rangle
BARE-V = {@TENSE(PRESENT)
    \neg@3SG
    \neg(\uparrow TENSE) }
```


## Templates: <br> Lexical entries and phrasal configurations

- Templates can be associated with lexical entries, but as they are just named descriptions, they can also be associated with c-structure configurations by calling the template in the c-structure rule.
- Example: English relative clauses have bare and non-bare alternatives
(I) the book Kim read
(2) the book which Kim read
- Suppose we have a template REL that captures the relativizing information.
- REL $=\lambda Q . \lambda P \cdot \lambda x . P(x) \wedge Q(x):$ clause $\multimap$ nominal $\multimap$ nominal
- This template can now be associated with a relative pronoun or with the rule for a bare/reduced relative clause
(3) which D @REL
(4) $\mathrm{CP} \longrightarrow\binom{\mathrm{RelP}}{\cdots} \quad\left(\begin{array}{c}\mathrm{C}^{\prime} \\ (\text { @REL })\end{array}\right.$


## Template hierarchies \& type hierarchies

- As we've seen, template definitions may contain reference to other templates.
- This effectively creates a hierarchy of templates, similar to the type hierarchies of Head-Driven Phrase Structure Grammar.
- Differences:
I. Type hierarchies represent relations between structures, whereas template hierarchies represent relations between descriptions of structures:Templates do not appear in the actual structures of the theory, but only in descriptions that the structures must satisfy.

2. Type hierarchies represent inheritance in an and/or semilattice.

- The daughters of a type represent disjoint subtypes (or).
- Multiple mothers for a type represent conjoined super- types (and).


## Template hierarchies \& type hierarchies

Type hierarchy: Inheritance


Template hierarchy: Inclusion

| 3SG | laughs | $\begin{aligned} & (\uparrow \text { PRED })=\text { 'laugh }\langle\text { SUBJ })^{\prime} \\ & \text { @3SG } \end{aligned}$ |
| :---: | :---: | :---: |
| laugh laughs | laugh | $(\uparrow$ PRED $)={ }^{\text {'laugh }}$ (SUBJ ${ }^{\prime}$ |
|  |  | $\checkmark$ @3SG |

## Glue Semantics

## Overview

- Glue Semantics is a method of semantic composition in which a potentially representationally rich meaning language is paired with a very constrained logic of composition that 'glues' pieces of meaning together to obtain larger meanings.
- You can think of the pieces of meaning like Lego pieces:They can only fit together in certain ways.
- The meaning language is some logic that supports the lambda calculus and has a modeltheoretic interpretation.
- The glue logic is (a fragment of) Linear Logic, a logic originally developed for theoretical computer science.
- Linear Logic, and hence the glue logic, is a resource logic:All meanings obtained through the syntactic parse must be used exactly once.
- It's like you have to use all your Lego pieces to build something and, obviously, no piece may be used more than once.


## Meaning constructors

- Meaningful linguistic expressions, particularly but not necessarily lexical items, are associated with meaning constructors of the following form:

$$
\mathcal{M}: G
$$

- The expression on the left is a term from the meaning language. The expression on the right is the associated term from the glue logic. The colon is an uninterpreted pairing symbol.


## The logic of implication: Filling in missing pieces

- Linear implication is a cute lollipop.
- We can define its logical behaviour in terms of two simple proof rules.

Functional application : Implication elimination (modus ponens)

```
\[
\frac{f: A \multimap B \quad a: A}{f(a): B} \multimap^{\mathcal{E}}
\]
```

Functional abstraction : Implication introduction (hypothetical reasoning)

$$
\begin{gathered}
{[a: A]^{1}} \\
\vdots \\
\frac{f: B}{\lambda a . f: A \multimap B}{ }^{\circ}{ }_{\mathcal{I}, 1}
\end{gathered}
$$

## Example:

## Kim hugged Robin

- Meaning constructors from lexical entries

| Kim | $e$ | kim $: \uparrow_{\sigma}$ |
| :--- | :--- | :--- |
| Robin | $e$ | robin: $\uparrow_{\sigma}$ |
| hugged | $e \rightarrow(e \rightarrow t)$ | $\lambda y \cdot \lambda x \cdot \operatorname{hug}(x, y):(\uparrow \mathrm{OBJ})_{\sigma} \multimap(\uparrow \mathrm{SUBJ})_{\sigma} \multimap \uparrow_{\sigma}$ |

- F-structure



## Example: Kim hugged Robin

- Instantiated meaning constructors

| Kim | $e$ | kim: $k_{\sigma}$ |
| :--- | :--- | :--- |
| Robin | $e$ | robin: $r_{\sigma}$ |
| hugged | $e \rightarrow(e \rightarrow t)$ | $\lambda y \cdot \lambda x \cdot \operatorname{lug}(x, y): r_{\sigma} \multimap k_{\sigma} \multimap h_{\sigma}$ |

- Proof

$$
\begin{aligned}
& \lambda y . \lambda x . \operatorname{hug}(x, y): r_{\sigma} \multimap k_{\sigma} \multimap h_{\sigma} \quad \text { robin }: r_{\sigma} \\
& (\lambda y \cdot \lambda x \cdot \operatorname{hug}(x, y))(\text { robin }): k_{\sigma} \multimap h_{\sigma} \\
& \lambda x \cdot \operatorname{hug}(x, \text { robin }): k_{\sigma} \multimap h_{\sigma} \quad \text { kim }: k_{\sigma} \\
& \frac{(\lambda x \cdot \operatorname{hug}(x, \text { robin }))(\text { kim }): h_{\sigma}}{\operatorname{hug}(\text { kim, robin }): h_{\sigma}} \Rightarrow_{\beta}
\end{aligned}
$$

## Flexible Composition

## Overview

- Flexible Composition is the name l've given to a theory of semantic composition, or more specifically how compositional meanings are packaged, that my collaborators (Mary Dalrymple, Gianluca Giorgolo, and Ida Toivonen) and I have been developing for a number of years.
- Basic intuition:Templates can be used to factor out common meanings across lexical items, e.g. argument structure regularities, and across phrasal configurations, e.g. so-called "constructional meanings" (but without actual constructions).


## Some features of Flexible Composition

I. The representation of core semantic information, such that the same lexical entry can be involved in a number of valency realizations
(I) The hamster ate a sheet of newspaper this morning.
(2) The hamster ate this morning.
(3) The hamster ate its way through a sheet of newspaper this morning.
2. The representation of missing/understood arguments
3. The representation of additional/derived arguments
(4) * The performer laughed the children.
(5) The performer laughed a funny laugh.
4. The possibility of associating meanings with syntactic configurations
(6) The performer sang the children a song.
5. Templates as generalizations over lexically encoded meaning
6. Templates as the locus of specification of meanings which can be associated with lexical entries or c-structure rules

## Some templates for Flexible Composition

```
Agent =
    @ ARG1
    \lambdaP\lambdax\lambdae.P(e) ^ agent (e)=x:
    [(\uparrow\sigma EVENT )}\multimap\mp@subsup{\uparrow}{\sigma}{}]\multimap(\mp@subsup{\uparrow}{\sigma}{}\mp@subsup{\mathrm{ ARG }}{1}{})\multimap(\mp@subsup{\uparrow}{\sigma}{}\mathrm{ EVENT })\multimap\mp@subsup{\uparrow}{\sigma}{
```

Patient $=$
@ARG2
$\lambda P \lambda x \lambda e . P(e) \wedge \operatorname{patient}(e)=x:$
$\left[\left(\uparrow_{\sigma}\right.\right.$ EVENT $\left.) \multimap \uparrow_{\sigma}\right] \multimap\left(\uparrow_{\sigma}\right.$ ARG $\left._{2}\right) \multimap\left(\uparrow_{\sigma}\right.$ EVENT $) \multimap \uparrow_{\sigma}$
AGENT-PATIENT $=$
@ AGENT
@PATIENT
PASSIVE $=$
$(\uparrow$ VOICE $)=$ PASSIVE
@ ADDMAP(PLUSR,ARG ${ }_{1}$ )
$\left(\lambda P \exists x \cdot[P(x)]:\left[\left(\uparrow_{\sigma} \mathrm{ARG}_{1}\right) \multimap \uparrow_{\sigma}\right] \multimap \uparrow_{\sigma}\right)$

## CognateObject

```
\(\lambda x \lambda P \lambda e . P(e) \wedge x=\varepsilon(e):\)
\((\uparrow \text { OBJ })_{\sigma} \multimap\left[\left(\uparrow_{\sigma}\right.\right.\) EVENT \(\left.) \multimap \uparrow_{\sigma}\right] \multimap\left(\uparrow_{\sigma}\right.\) EVENT \() \multimap \uparrow_{\sigma}\)
```

Benefactive $=$
@ARG3
$\lambda x \lambda y \lambda$ Pe. $P(y)(e) \wedge$ beneficiary $(e)=x$ :
$\left(\uparrow_{\sigma} \mathrm{ARG}_{2}\right) \multimap\left(\uparrow_{\sigma} \mathrm{ARG}_{3}\right) \multimap\left[\left(\uparrow_{\sigma} \mathrm{ARG}_{2}\right) \multimap\left(\uparrow_{\sigma}\right.\right.$ EVENT $\left.) \multimap \uparrow_{\sigma}\right] \multimap\left(\uparrow_{\sigma}\right.$ EVENT $) \multimap \uparrow_{\sigma}$

UnDERSTOODOBJECT $=$
$\lambda P \exists x \cdot[P(x)]:\left[\left(\uparrow_{\sigma} \mathrm{ARG}_{2}\right) \multimap \uparrow_{\sigma}\right] \multimap \uparrow_{\sigma}$

```
PAST =
    (\uparrow TENSE) = PAST
    \lambdaP\existse.[P(e) ^ past(e)]:
```



## Example:

## Kim was crushed last night


crushed V

$$
\begin{aligned}
& (\uparrow \text { PRED })=\text { 'crush' } \\
& @ \text { AGENT-PATIENT } \\
& \{\text { @PAST } \mid @ \text { PASSIVE }\} \\
& \lambda e . c r u s h ~ \\
& (e):\left(\uparrow_{\sigma} \text { EVENT }\right) \multimap \uparrow_{\sigma}
\end{aligned}
$$

## Example:

## Kim was crushed by Godzilla last night

| PRED | 'crush' |  | [REL crush |
| :---: | :---: | :---: | :---: |
| SUBJ | $[\text { PRED 'Kim'] }$ | $\chi_{\sigma}$ | EVENT ev[] |
| OBL | $\left[\begin{array}{lll} \text { PRED } & \text { 'by' } & \\ \text { OBJ } & \text { PRED } & \text { 'Godzilla' } \end{array}\right]$ |  | $\left[\begin{array}{ll}\mathrm{ARG}_{1} & g \\ \mathrm{ARG}_{2} & k\end{array}\right]$ |
| ADJ | $\{[" \text { last night" }]\}$ | $\sigma$ |  |
| TENSE | PAST |  |  |
| VOICE | PASSIVE |  |  |
| by P | $(\uparrow$ PRED $)=$ 'by' |  |  |
|  | $((\mathrm{OBL} \uparrow) \mathrm{VOICE})={ }_{c}$ PASSIVE |  |  |
|  | $(\uparrow \mathrm{OBJ})_{\sigma}=\left((\mathrm{OBL} \uparrow)_{\sigma} \mathrm{ARG}_{1}\right)$ |  |  |
|  | $\lambda x \lambda P \cdot[P(x)]:\left(\uparrow_{\sigma} \mathrm{ARG}_{1}\right) \multimap\left[\uparrow_{\sigma}\right.$ | $\left.\multimap(\mathrm{OBL} \uparrow)_{\sigma}\right]$ | $\multimap(\mathrm{OBL} \uparrow)_{\sigma}$ |

## Example:

## Kim laughed a crazy laugh



## Example:

## Kim drew Godzilla for Sandy



## Example:

## Kim drew Sandy Godzilla



Note: It is a normal assumption in LFG that elements of c-structure rules are optional. This rule therefore allows the passive verb to be inserted underV. (It would also have to have a PP node added for the oblique, but this is a trivial modification.)

## Proof:

## Kim was crushed last night



## What just happened?

- Overview of Lexical-Functional Grammar
- Overview of Glue Semantics
- Introduction to Flexible Composition as an approach to argument structure

Thank you

## Some key references

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